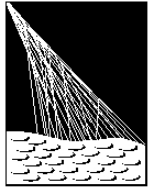


# Overview of hadronic interaction studies at the Pierre Auger Observatory



PIERRE  
AUGER  
OBSERVATORY

Jakub Vicha\* for the Pierre Auger Collaboration

\*FZU - Institute of Physics of the Czech Academy of Sciences, Prague

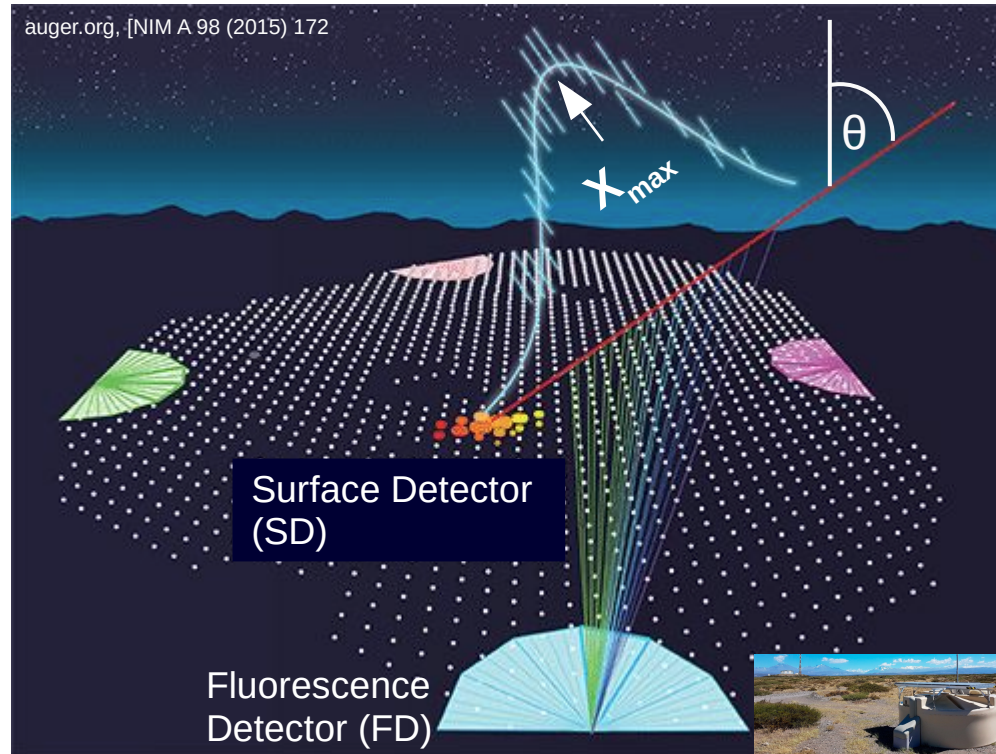


vicha@fzu.cz

# The Pierre Auger Observatory - *the best instrument to study hadronic interactions above $\sqrt{s} \approx 50$ TeV*

## SD signal

- **muon content**
  - from buried scintillators,  $\theta < 45^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$
- **muon production depth**
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$
- **muon energy spectrum**
  - from attenuation with  $\theta$  and  $r$
- **rise time** of signal vs.  $r$



*see details about hadronic interactions in the R. Conceicao's invited review*

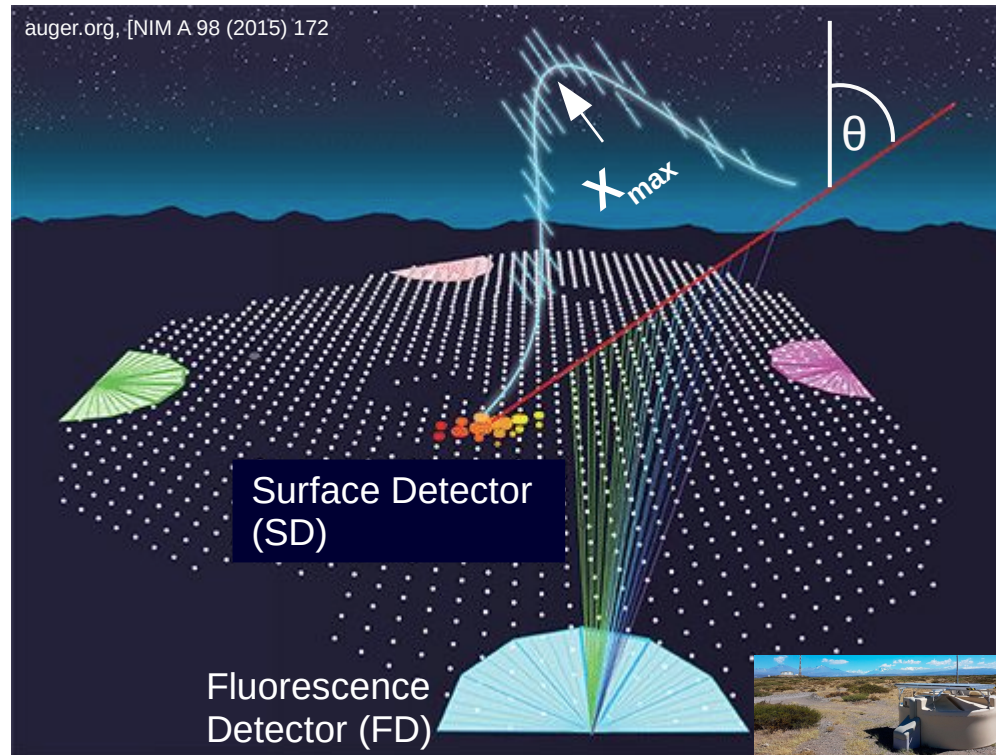
## FD longitudinal profile

- estimation of **primary masses** from  $X_{\text{max}}$  fits
- interpretation of  $X_{\text{max}}$  moments using  $\ln A$
- **p-air cross-section** from tail of  $X_{\text{max}}$  distribution
- **average shape** of longitudinal profiles
- frequency of **anomalous showers**

# The Pierre Auger Observatory - *the best instrument to study hadronic interactions above $\sqrt{s} \approx 50$ TeV*

## SD signal

- muon content
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    - [Phys. Rev. D 90 (2014) 012012]
  - muon energy spectrum
    - from attenuation with  $\theta$  and  $r$
  - rise time of signal vs.  $r$ 
    - [Phys. Rev. D 96 (2017) 122003]
- + neutrons in SSDs,  
see talk of T. Schulz

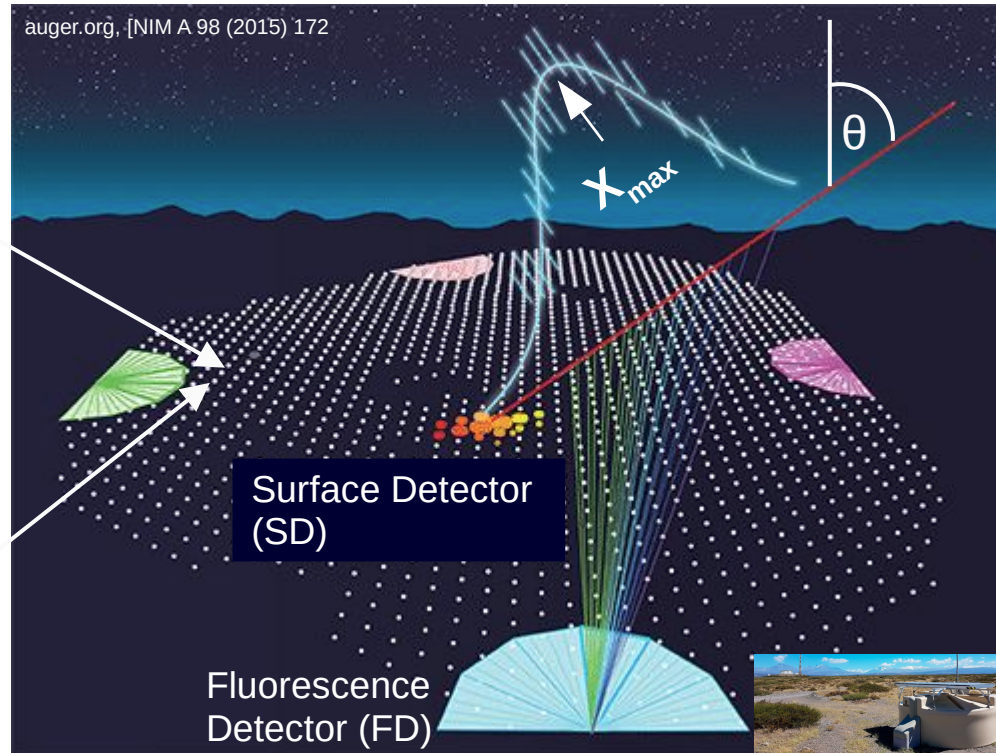
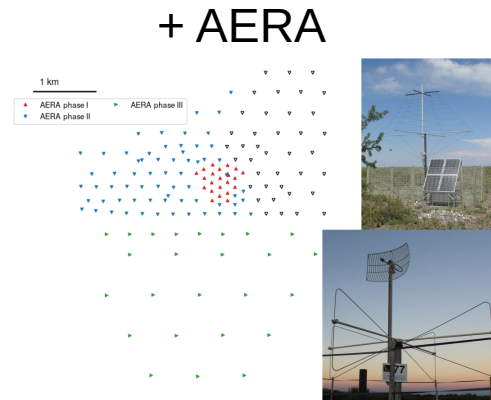
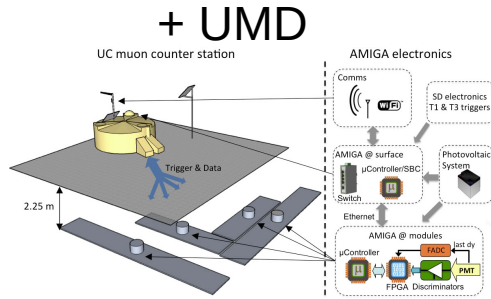


*not covered here,  
see references*

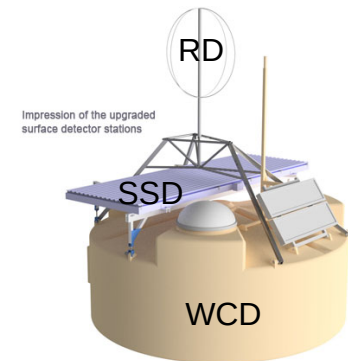
## FD longitudinal profile

- estimation of primary masses from  $X_{\text{max}}$  fits
- interpretation of  $X_{\text{max}}$  moments using  $\ln A$
- p-air cross-section from tail of  $X_{\text{max}}$  distribution
- average shape of longitudinal profiles
  - [JCAP 03 (2019) 018]
- frequency of anomalous showers
  - [EPJ Web of Conferences 144 (2017) 01009]

# The Pierre Auger Observatory - *the best instrument to study hadronic interactions above $\sqrt{s} \approx 50$ TeV*



**+ AugerPrime**



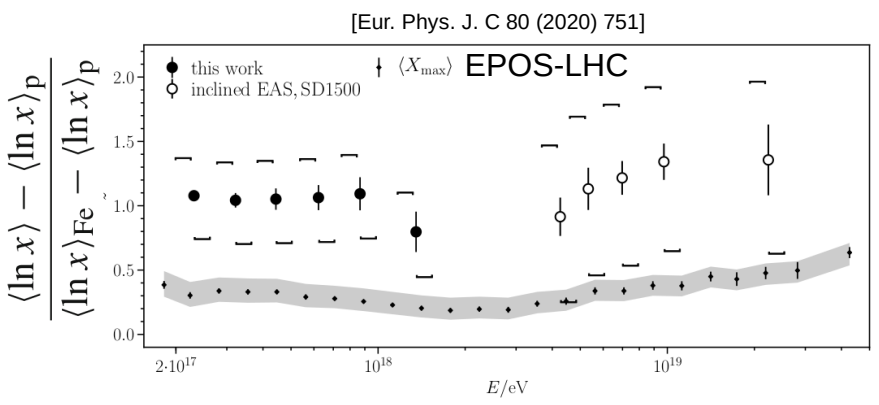
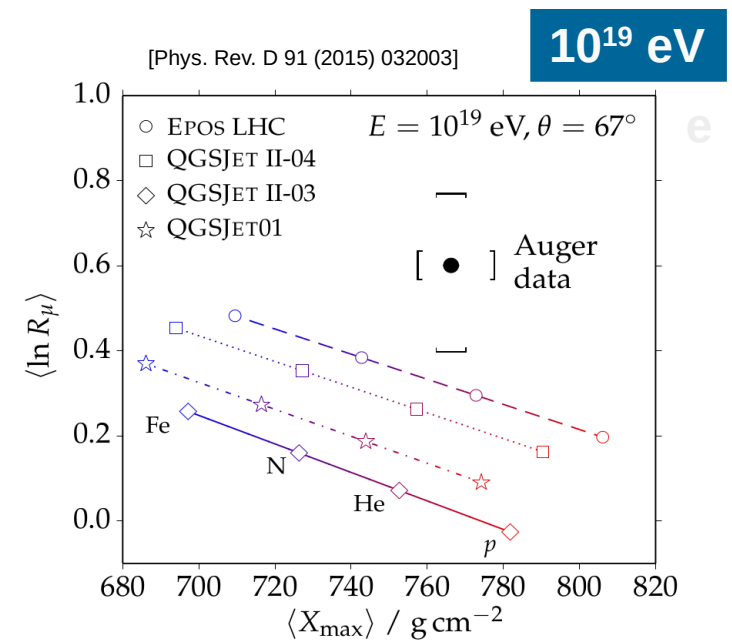
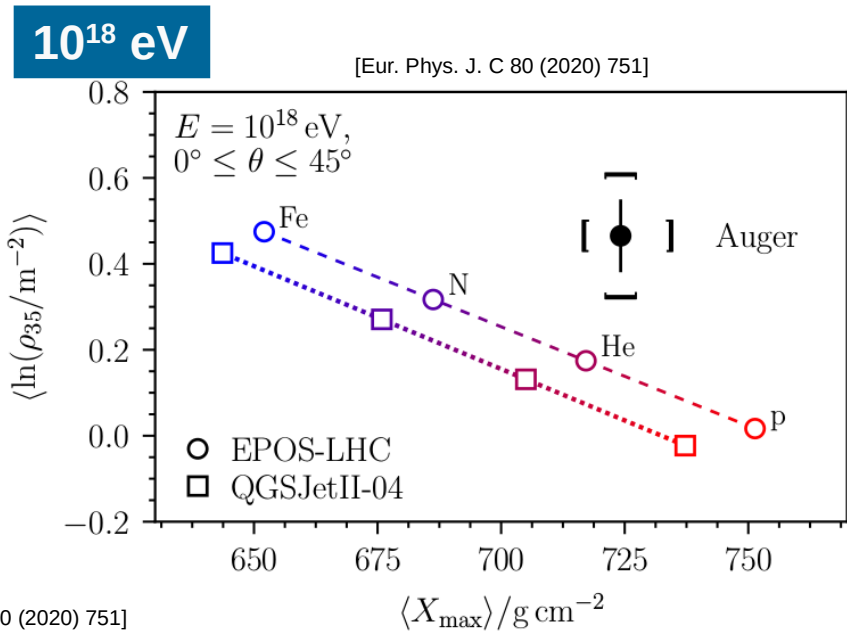
**Especially for combination of SD and FD observables !**

# Observables relevant to hadronic interaction models

## SD signal

- muon content
  - from buried scintillators,  $\theta < 45^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$

• muon production depth  
 → for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$



- $\sim 2\text{-}3\sigma$  problem to describe the size of the muon content: **factor  $\sim 1.3\text{-}1.6$  !**
- problem seen at various energies and zenith angles

• range shape of longitudinal profiles  
 • frequency of anomalous showers

# Observables relevant to hadronic interaction models

## SD signal

- muon content
  - from buried scintillators,  $\theta < 45^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$
- muon production depth
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$
- muon energy spectrum
  - from attenuation with  $\theta$  and  $r$
- rise time of signal vs.  $r$

- very hard in general with SD only
  - large systematics from energy scale
  - multi-detector approach necessary:
    - SD+FD at different zenith angles
    - WCD+RPC+SSD+UMD+RD
- @ AugerPrime

see R. Conceicao's  
invited review

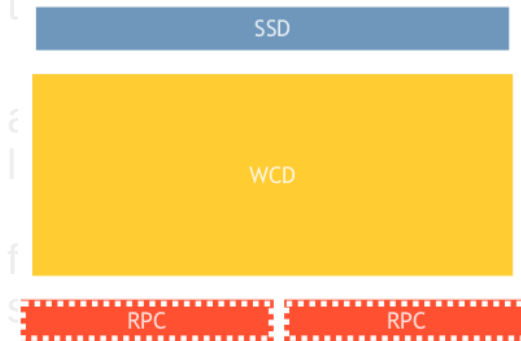
+ Underground  
Muon Detector

FD longitudinal profile

estimation of primary masses from  $X_{\text{max}}$  fits

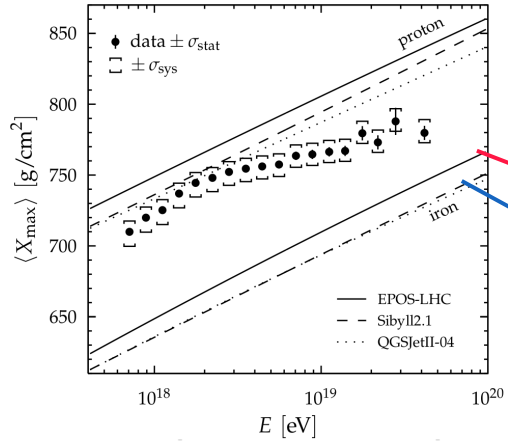
interpretation of  $X_{\text{max}}$  moments using  $\ln A$

+ Radio Detector

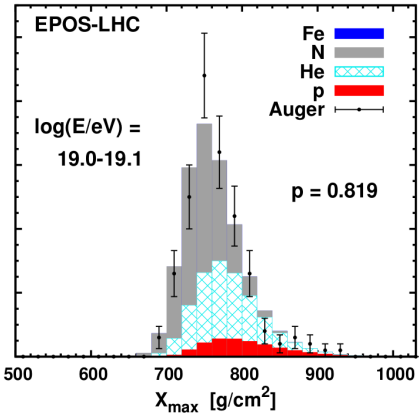


# Observables relevant to hadronic interaction models

[Phys. Rev. D 90 (2014) 122005]

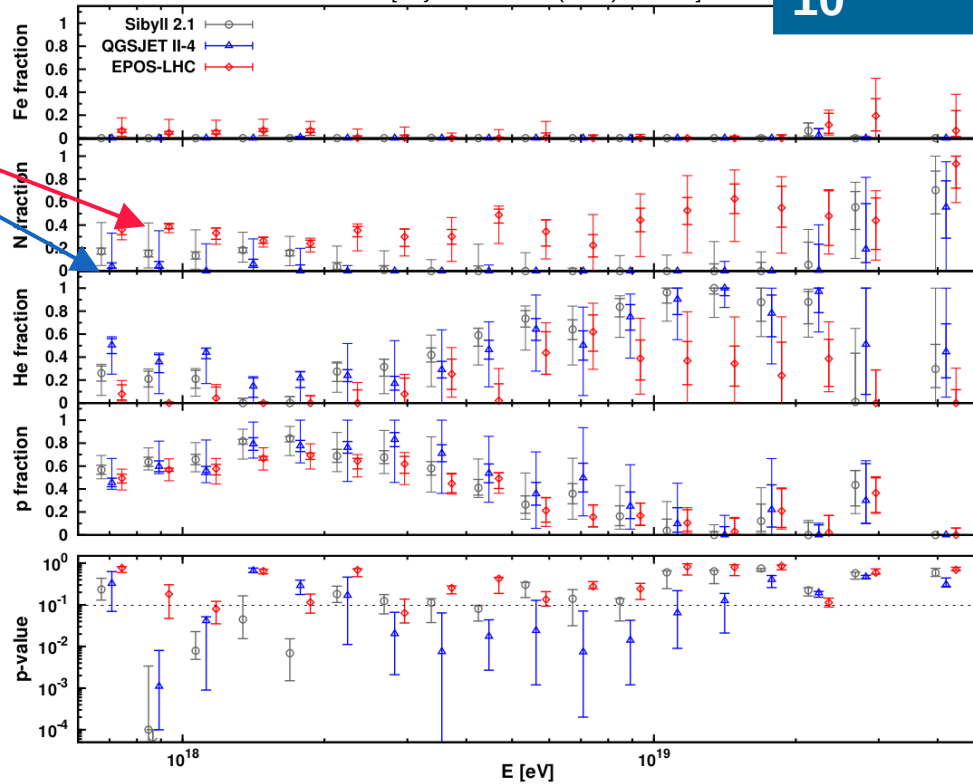


→ for core distance



[Phys. Rev. D 90 (2014) 122006]

**10<sup>17.8-19.6</sup> eV**



## FD longitudinal profile

- estimation of primary masses from  $X_{\max}$  fits

• dependent on MC  $X_{\max}$  scale  
 - input into many hadronic interaction studies

- average shape of longitudinal profiles
- frequency of anomalous showers

see talk of T. Fitoussi for update

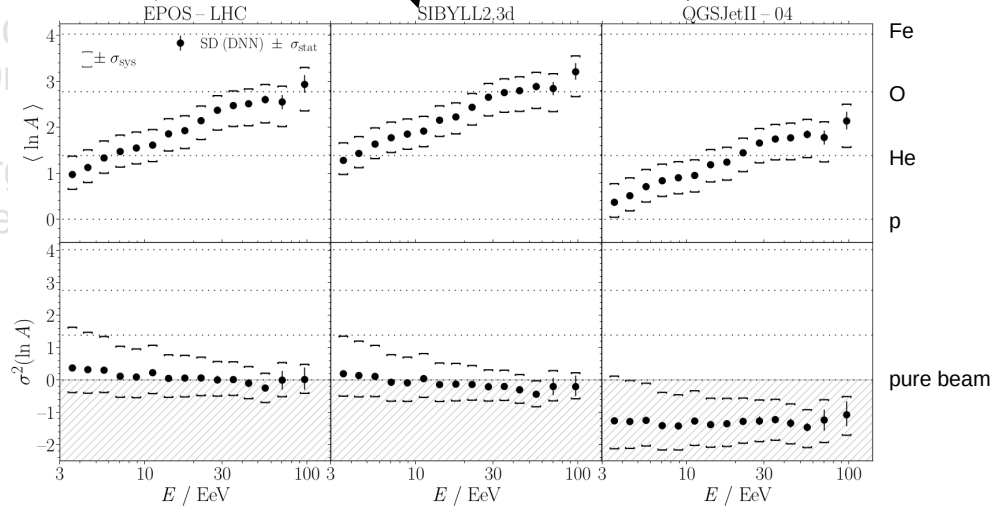
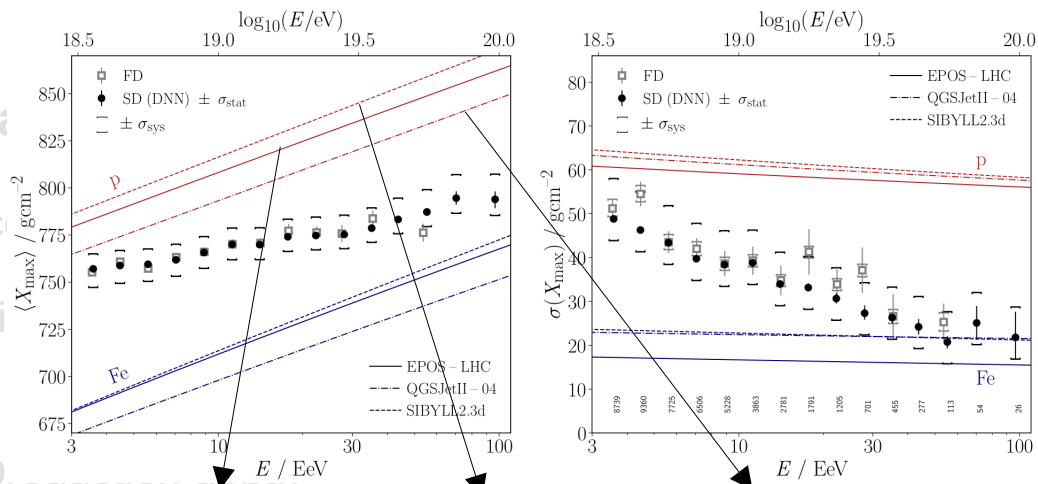
# Observables relevant to hadronic interaction models

[accepted in PRD, arXiv:2406.06319]

**10<sup>18.5-20.0</sup> eV**

## FD longitudinal profile

- estimation of primary masses from  $X_{\max}$  fits
- interpretation of  $X_{\max}$  moments using  $\ln A$



$$\langle \ln A \rangle = \frac{\langle X_{\max} \rangle - \langle X_{\max} \rangle_p}{f_E}$$

$$\sigma_{\ln A}^2 = \frac{\sigma^2(X_{\max}) - \sigma_{\text{sh}}^2(\langle \ln A \rangle)}{b \sigma_p^2 + f_E^2}$$

[JCAP 02 (2013) 026]

**Strong dependence on the MC  $X_{\max}$  scale**

- SD signal
- muon count
- from sci
- from
- muon p
- for core ( $r > 1500$ )
- muon energy
- from  $\theta$  and  $r$



# Observables relevant to hadronic interaction models

[accepted in PRD, arXiv:2406.06319]

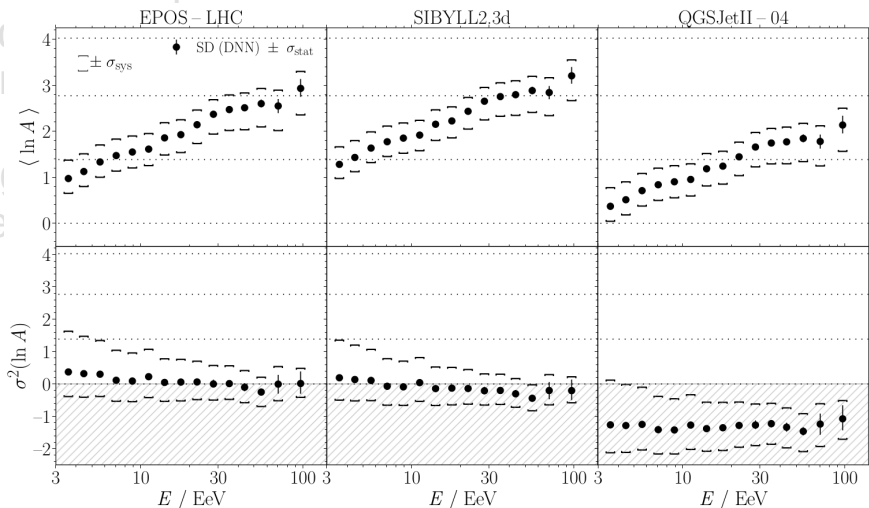
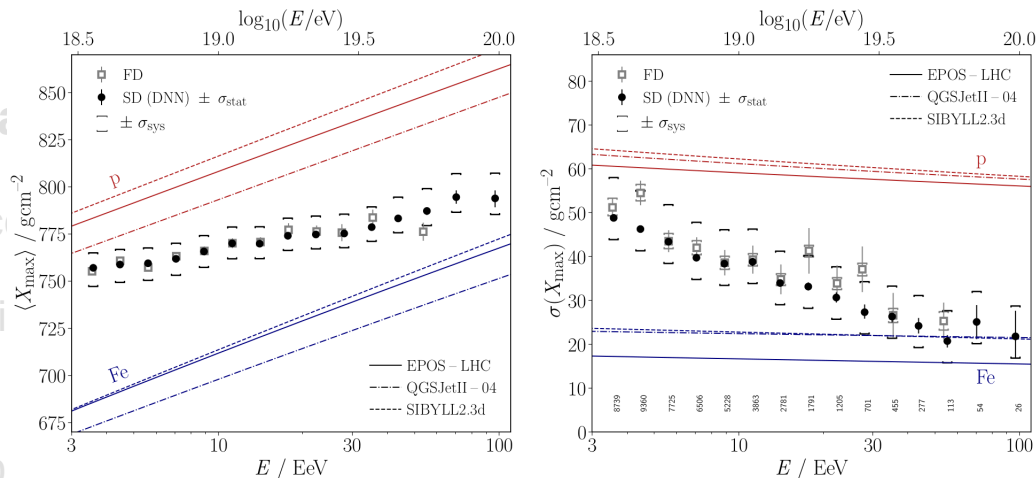
**10<sup>18.5-20.0</sup> eV**

## FD longitudinal profile

- estimation of primary masses from  $X_{\max}$  fits
- interpretation of  $X_{\max}$  moments using  $\ln A$
- p-air cross-section from tail of  $X_{\max}$  distribution

**Indication of too shallow predictions of  $\langle X_{\max} \rangle$  for all three models !**

showers



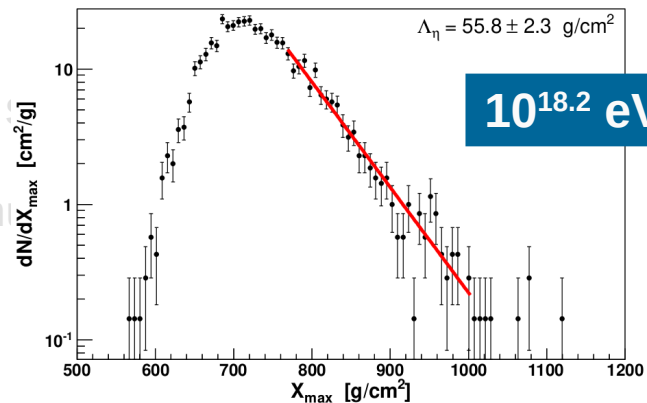
- SD signal
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- from sci
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- for core ( $r > 1500$ )
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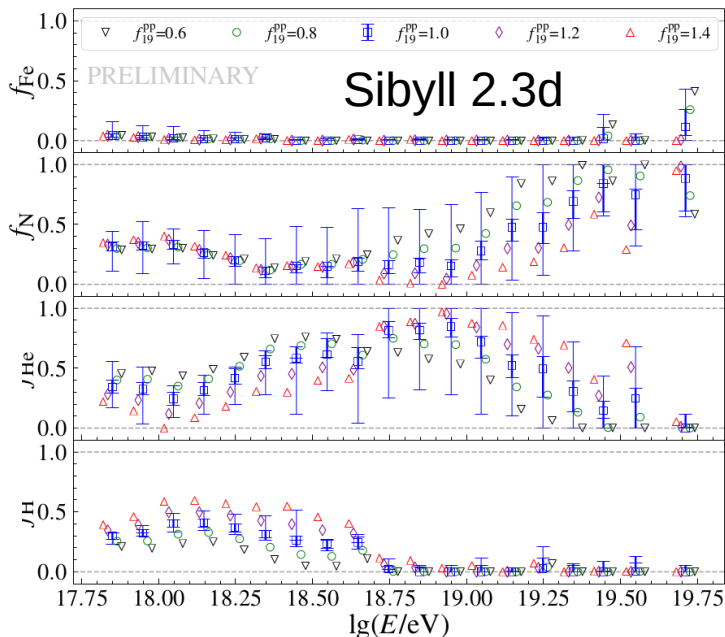
# Observables relevant to hadronic interaction models

[Phys. Rev. Lett. 109 (2012) 062002]

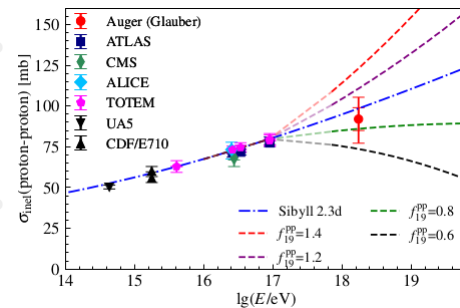


**10<sup>17.7-19.8</sup> eV ?**

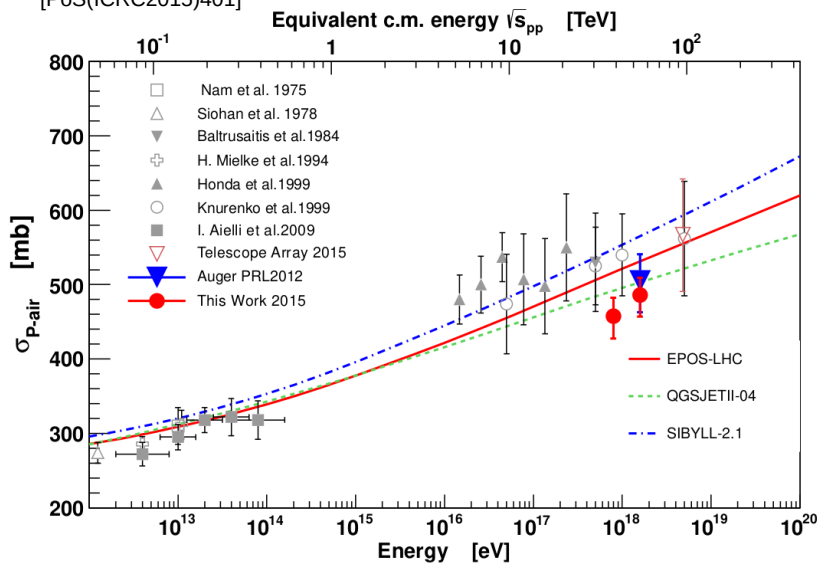
[PoS(ICRC2023)438]



## FD longitudinal profile



[PoS(ICRC2015)401]



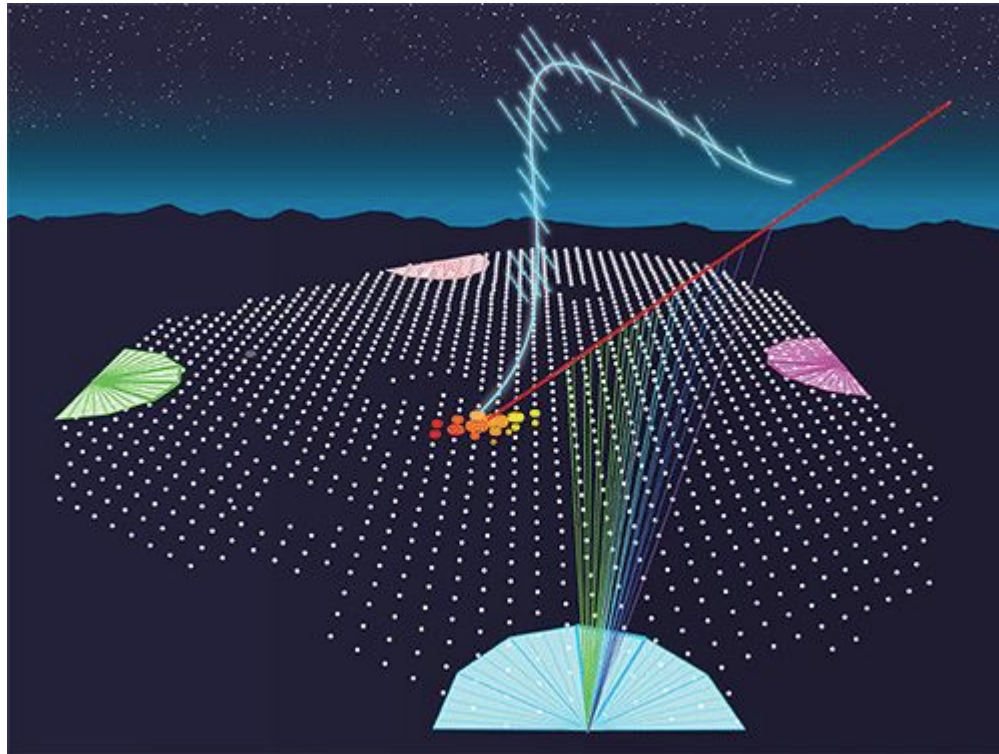
- **p-air cross-section** from tail of  $X_{\text{max}}$  distribution

- average shape of longitudinal profiles
- frequency of anomalous showers

- p-air cross-section consistent with current models
- **new approach:** composition+cross-section fit (decrease of systematics from He and  $X_{\text{max}}$  scale)

see *O. Tkachenko's talk*

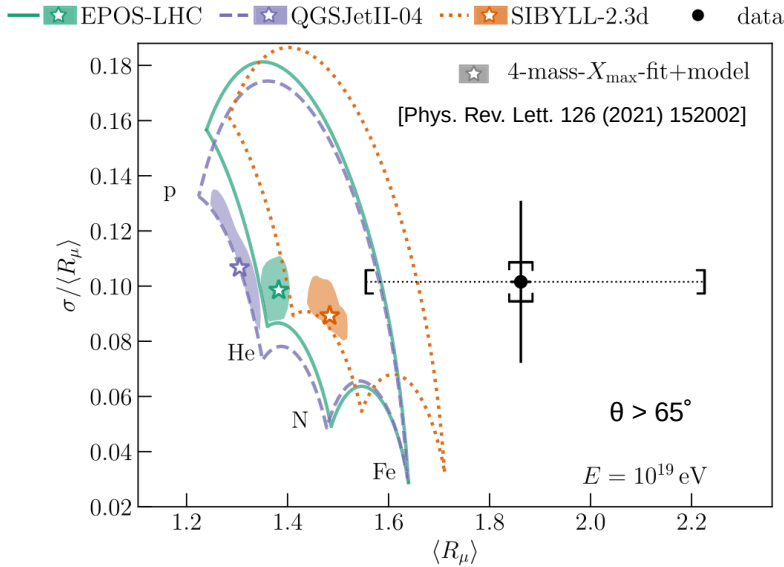
# Combining SD and FD observables



## Ground signal + Longitudinal profile

- inclined showers + FD  $\rightarrow \sigma(N_\mu)$
- correlation between  $X_{\max}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}}$
- applying shower-universality approach  $\rightarrow R_{\text{had}}$
- 2-dim distributions  $[S(1000), X_{\max}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\max}$

# Combining SD and FD observables

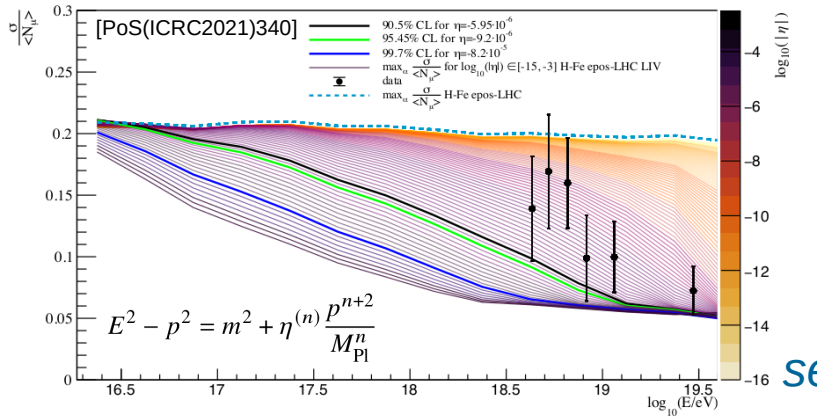


## Ground signal + Longitudinal profile

- inclined showers + FD  $\rightarrow \sigma(N_\mu)$  ~10<sup>18.6-19.5</sup> eV

- correlation between  $X_{\max}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}}$

- confirmation of a problem to describe the size of the muon content: **factor ~1.3-1.6**
- muon fluctuations are consistent with data (no obvious problem in the first interaction)   
  $\rightarrow$  Strong constraints on the Lorentz invariance violation (journal publication in preparation)



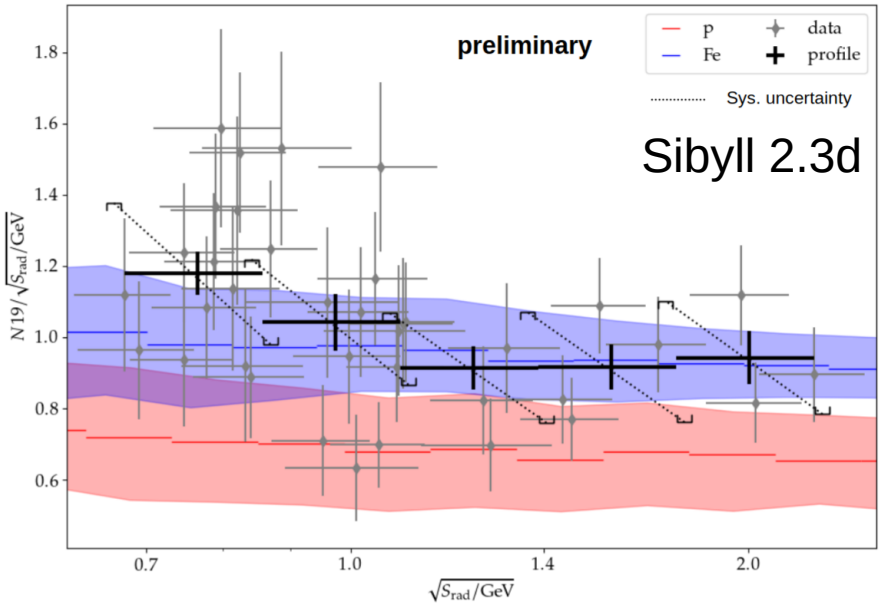
see talk of O. Deligny

# Combining SD and FD observables

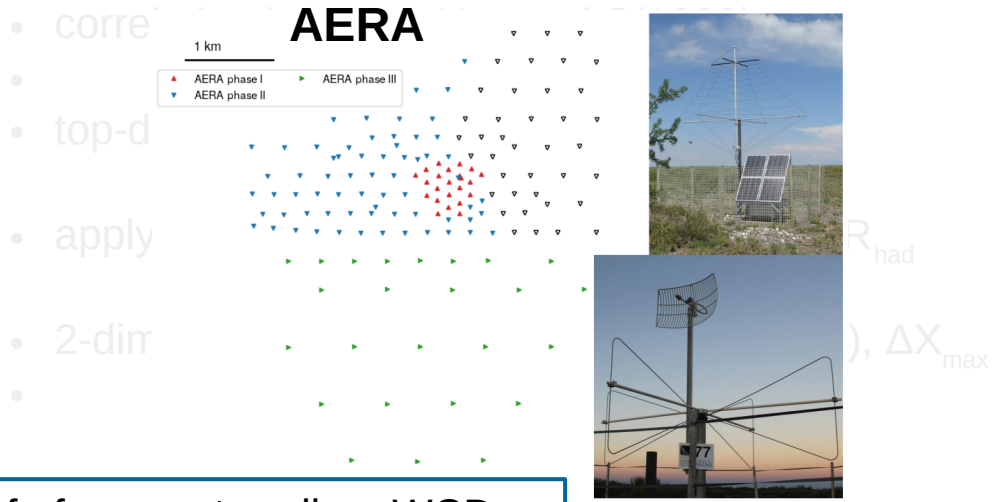
## Ground signal + Longitudinal profile

$\sim 10^{18.6-19.5}$  eV

- inclined showers + RD  $\rightarrow \langle N_\mu \rangle$  [PoS(ICRC2023)345]



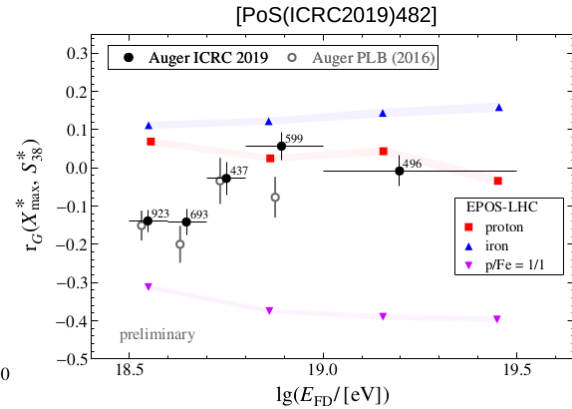
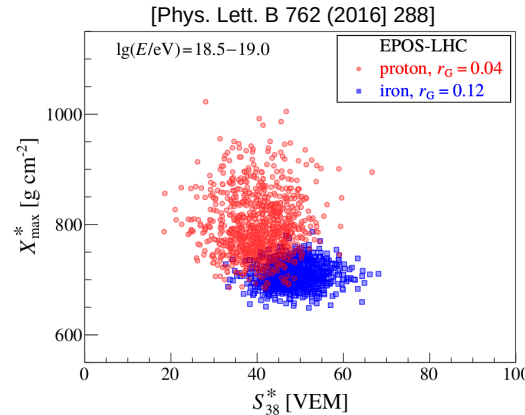
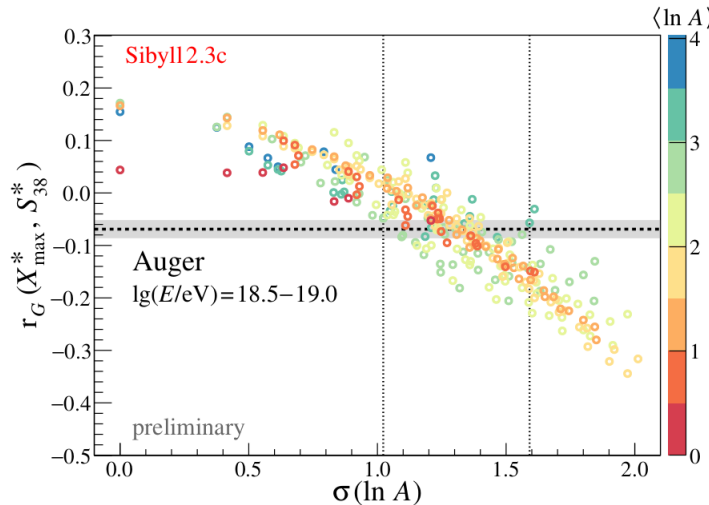
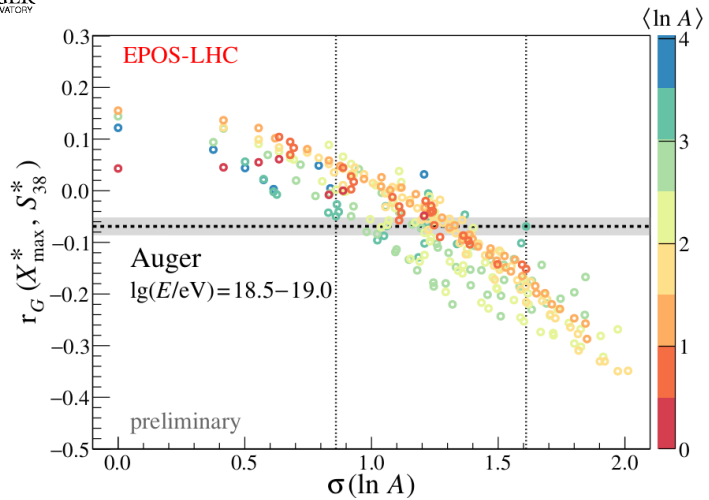
see M. Gottowik's poster



- proof of concept: radio + WCD
- muon scale compatible with previous results
- journal publication in preparation

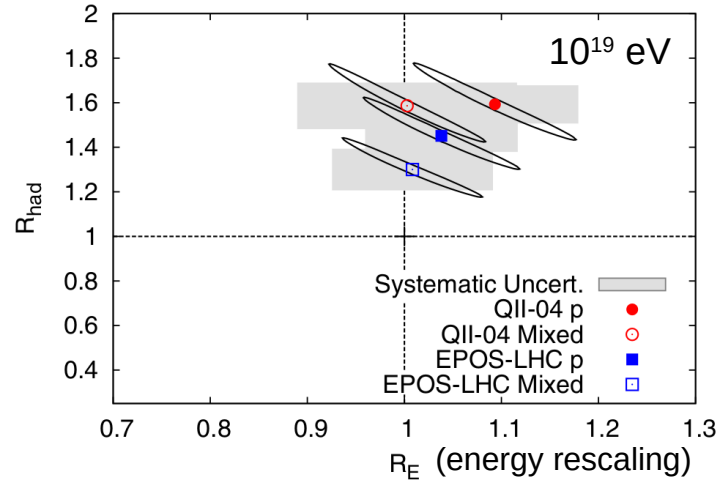
## Ground signal + Longitudinal profile

- inclined showers + FD →  $\sigma(N_{\nu})$
- correlation between  $X_{\max}$  and  $S(1000)$

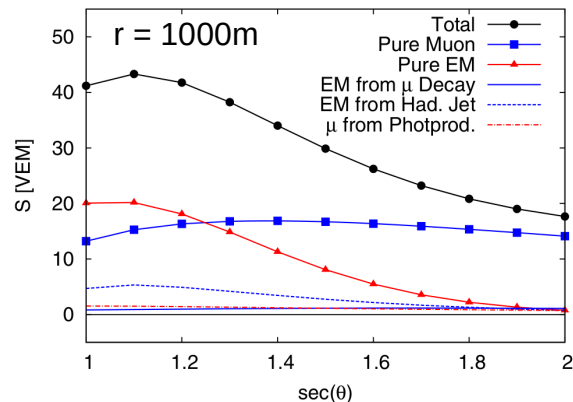


- ~model-independent estimator of spread of beam masses
- >5 $\sigma$  tension with light masses from  $X_{\max}$  fits for QGSJet II-04 (too shallow  $X_{\max}$  scale)

# Combining SD and FD observables



$$S_{\text{resc}}(R_E, R_{\text{had}})_{i,j} \equiv R_E S_{\text{EM},i,j} + R_{\text{had}} R_E^\alpha S_{\text{had},i,j}$$



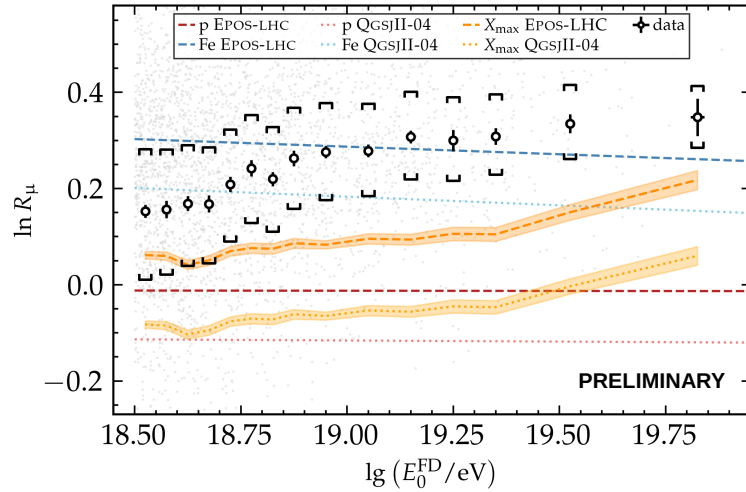
## Ground signal + Longitudinal profile

- inclined showers + FD  $\rightarrow \sigma(N_\mu)$
- correlation between  $X_{\text{max}}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}} \sim \mathbf{1.3 - 1.6 !}$
- [Phys. Rev. Lett. 117 (2016) 192001]
- applying shower-universality approach  $\rightarrow R_{\text{had}}$
- 2-dim distributions  $[S(1000), X_{\text{max}}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\text{max}}$

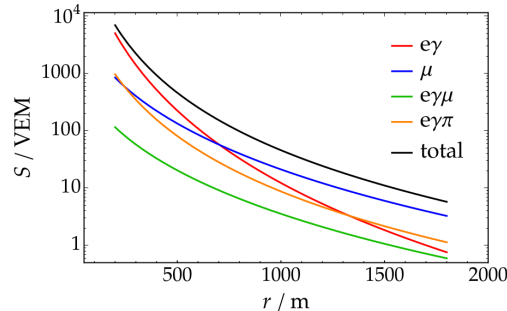
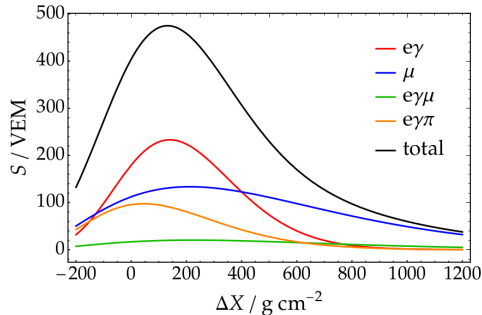
- mass from measured  $X_{\text{max}}$  - depends on MC  $X_{\text{max}}$  scale
- $\sim 2-3\sigma$  tension with strong dependence on energy scale

# Combining SD and FD observables

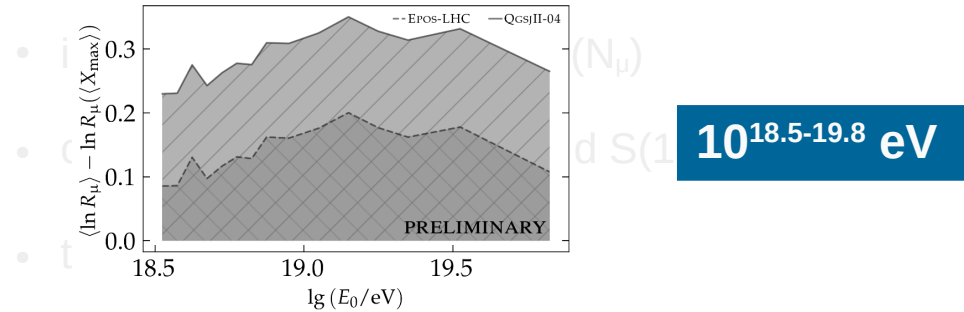
shower geometry, energy and  $X_{\max}$  from FD



$$S_{\text{tot}} \approx S_{e\gamma} + R_{\mu} (S_{\mu} + S_{e\gamma(\mu)} + S_{e\gamma(\pi)})$$



## Ground signal + Longitudinal profile



$10^{18.5-19.8}$  eV

- applying shower-universality approach  
 $\rightarrow R_{\text{had}} \sim \mathbf{1.1 - 1.3}$  [PoS(ICRC2023)339, arXiv:2405.03494]
- 2-dim c *see poster of M. Stadelmaier*

- $\sim 2\sigma$  tension
- $R_{\text{had}}$  smaller than in top-down approach
- $\sim$ insensitive to the MC  $X_{\max}$  scale
- journal publication in preparation





PIERRE AUGER OBSERVATORY

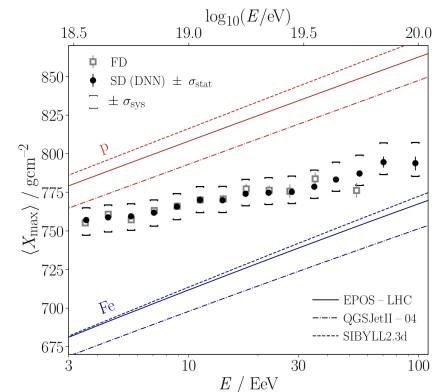
# Mass composition & tests of hadronic interactions

[accepted in PRD, arXiv:2406.06319]

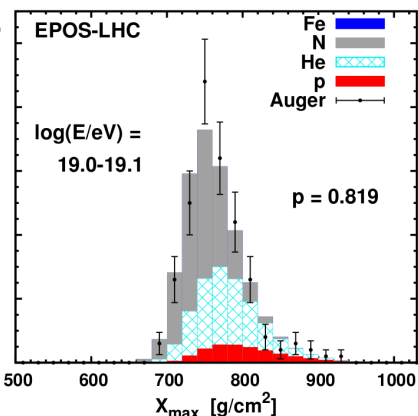
[Phys. Rev. D 90 (2014) 122006]

[Phys. Rev. Lett. 117 (2016) 192001]

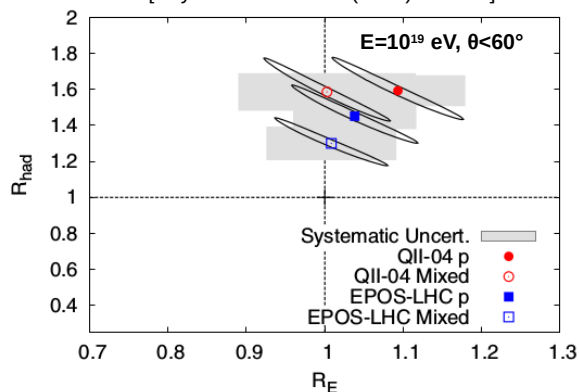
[Phys. Lett. B 762 (2016) 288]



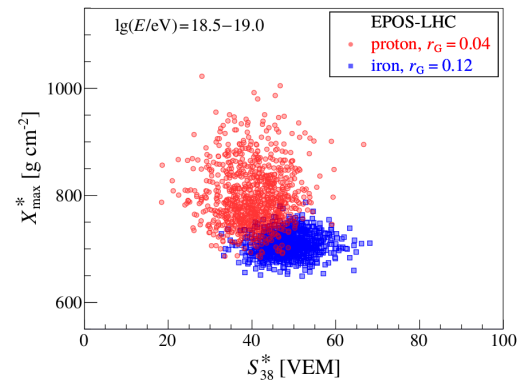
MC  $X_{\max}$  scale ?



Primary fraction fit



Deficit in MC hadronic signal



~ model-independent estimation of beam mixing from  $[X_{\max}, S(1000)]$  correlation

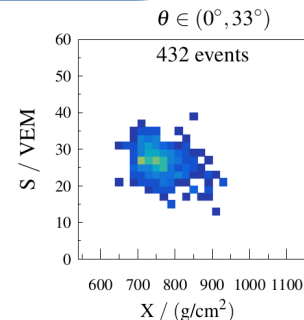
MC:

$$S_{\text{had}}(\theta) \rightarrow S_{\text{had}}(\theta) \cdot R_{\text{had}}(\theta)$$

$$X_{\max} \rightarrow X_{\max} + \Delta X_{\max}$$

[Phys. Rev. D 109 (2024) 102001]

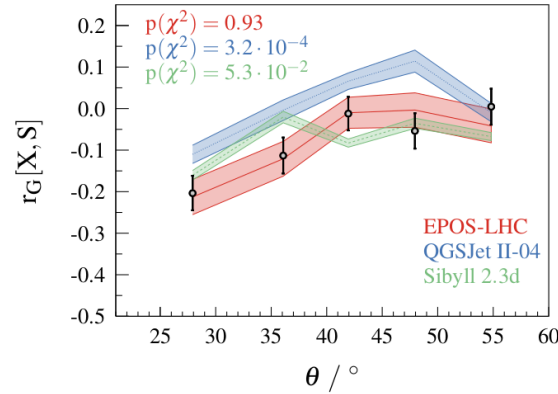
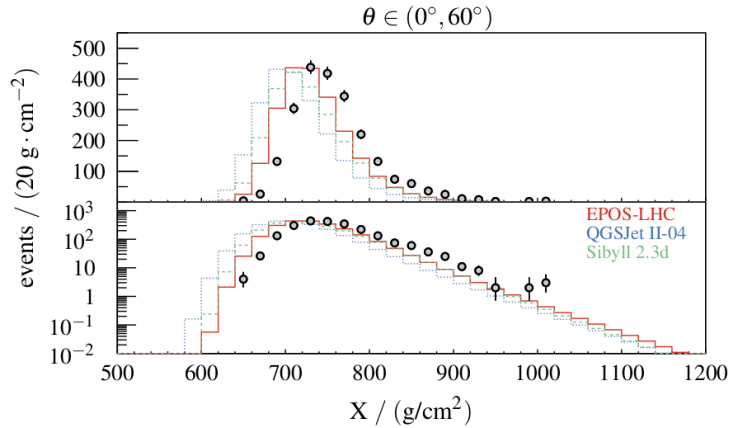
Mass composition fit of observed  $[X_{\max}, S(1000)](\theta)$  distributions with free modification of MC predictions **not only of hadronic signal but also of  $X_{\max}$**



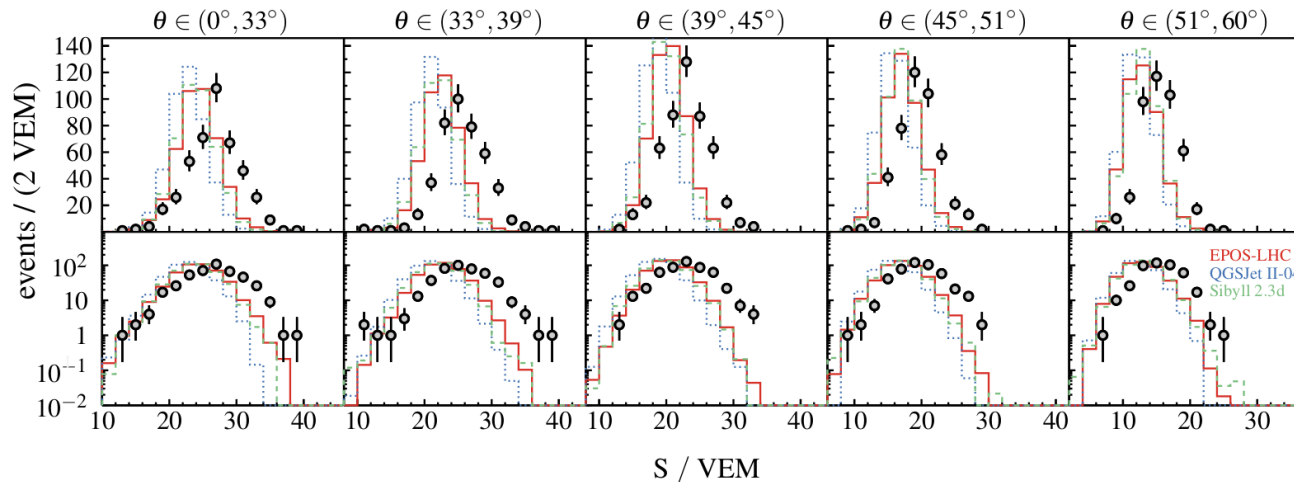
# Improvement in data description

$10^{18.5-19.0}$  eV

[Phys. Rev. D 109 (2024) 102001]



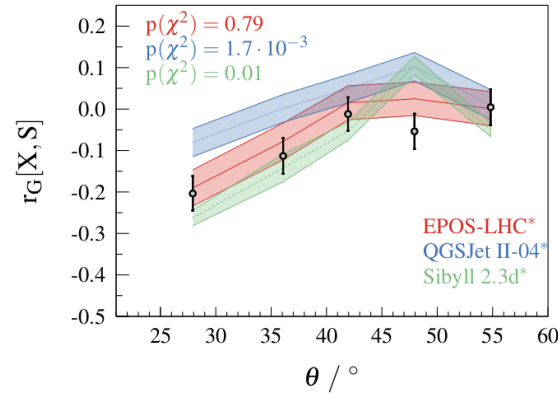
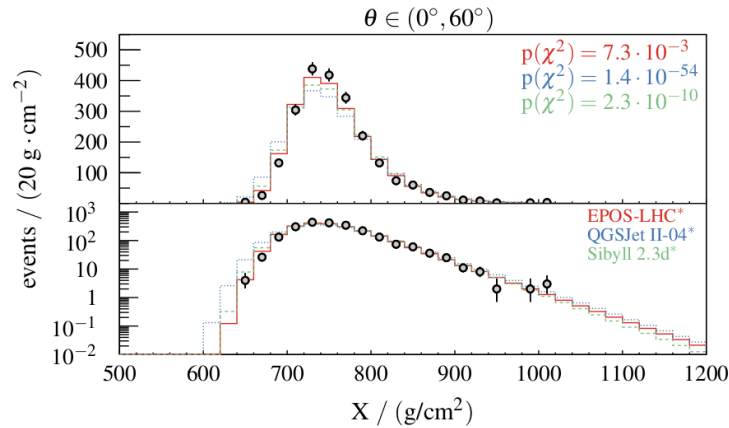
$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
none	2022.9	4508.0	2496.5
$\Delta X_{\max}$	738.6	1674.8	1015.7
$R_{\text{had}} = \text{const.}$	489.2	684.4	521.6
$R_{\text{had}}(\theta)$	489.2	673.9	517.6
$R_{\text{had}} = \text{const. and } \Delta X_{\max}$	452.2	486.7	454.2
$R_{\text{had}}(\theta) \text{ and } \Delta X_{\max}$	451.9	476.3	451.6



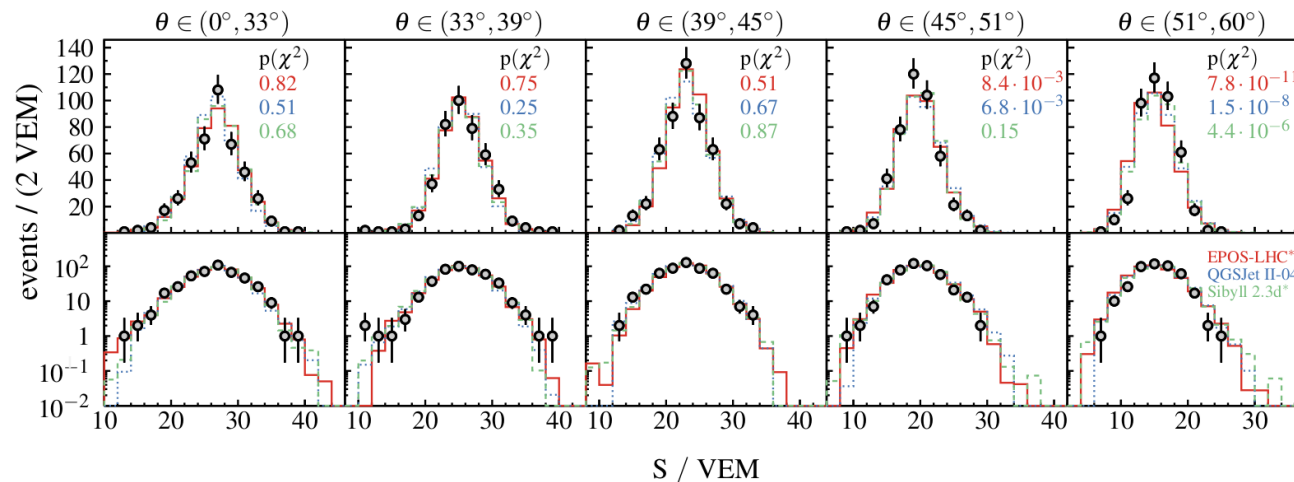
# Improvement in data description

$10^{18.5-19.0}$  eV

[Phys. Rev. D 109 (2024) 102001]



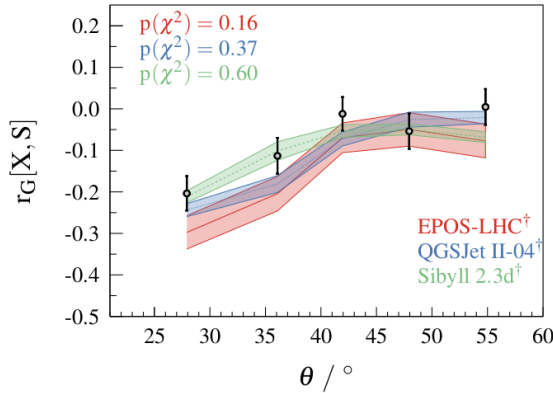
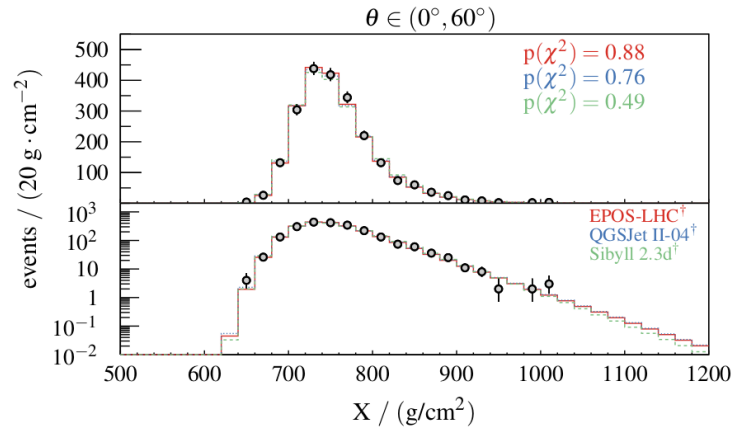
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# Improvement in data description

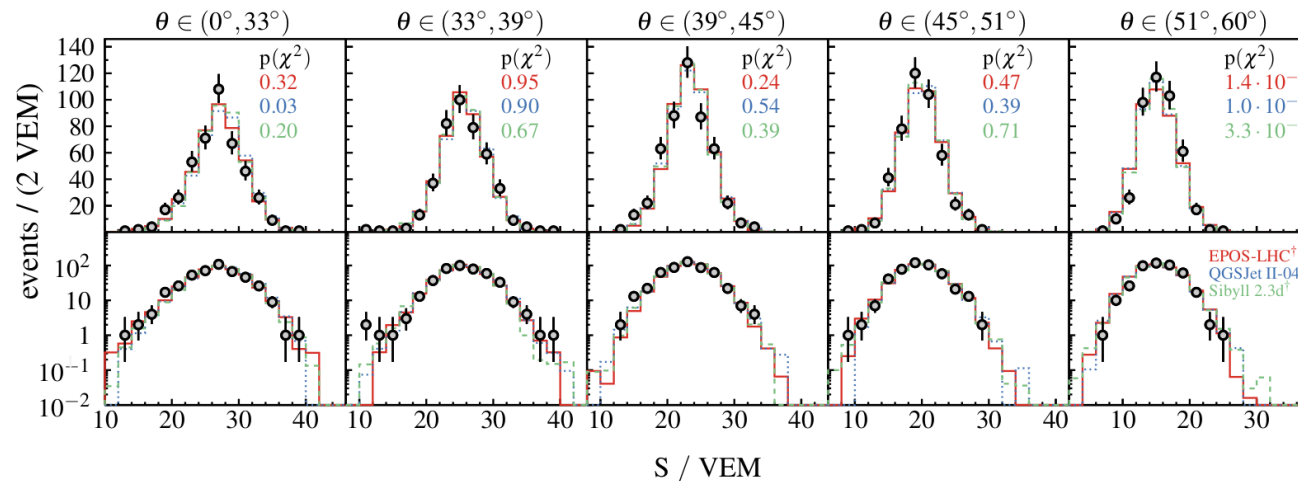
$10^{18.5-19.0}$  eV

[Phys. Rev. D 109 (2024) 102001]



*p-values of fits from MC-MC tests > 10% for all three models*

$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
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$\Delta X_{\max}$	738.6	1674.8	1015.7
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$R_{\text{had}}(\theta)$	489.2	673.9	517.6
$R_{\text{had}} = \text{const. and } \Delta X_{\max}$	452.2	486.7	454.2
$R_{\text{had}}(\theta)$ and $\Delta X_{\max}$	451.9	476.3	451.6



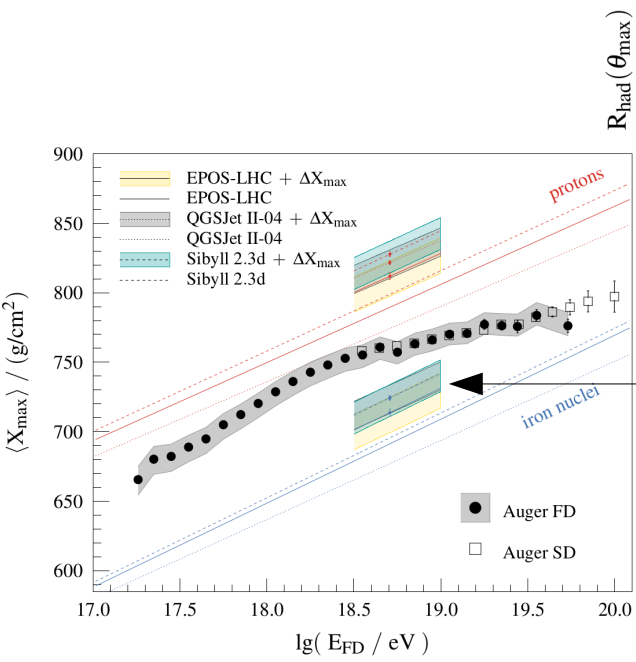
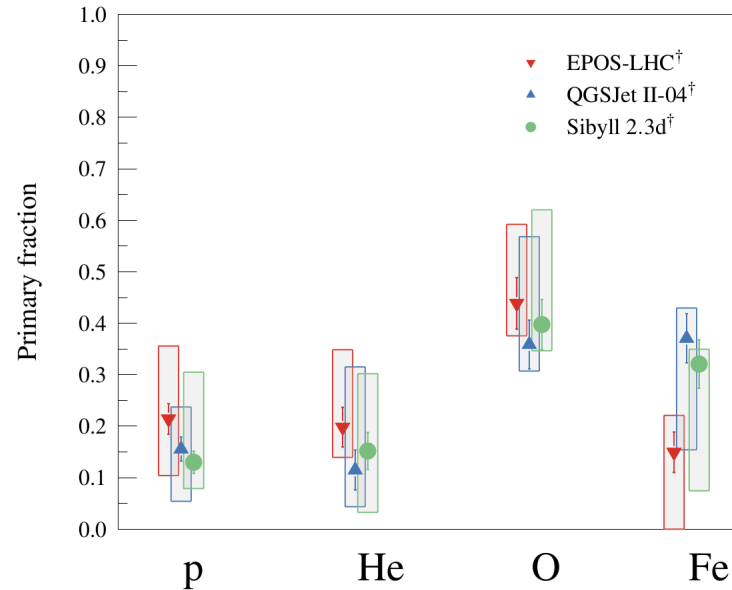
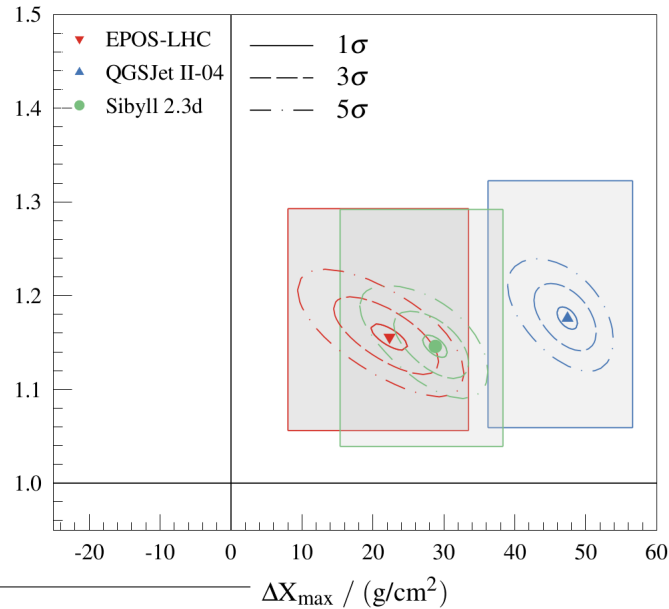
Significant improvement  $>5\sigma$  using  $R_{\text{had}}$  and  $\Delta X_{\max}$  (Likelihood ratio tests for nested model using Wilks' theorem)

# Fitted parameters

[Phys. Rev. D 109 (2024) 102001]

Zenith dependence of  $R_{\text{had}}$  assumed to be

linear in  $X_{\text{ground}} - X_{\text{max}}$   
 $\rightarrow R_{\text{had}}(\theta_{\text{min}} \sim 28^\circ), R_{\text{had}}(\theta_{\text{max}} \sim 55^\circ)$

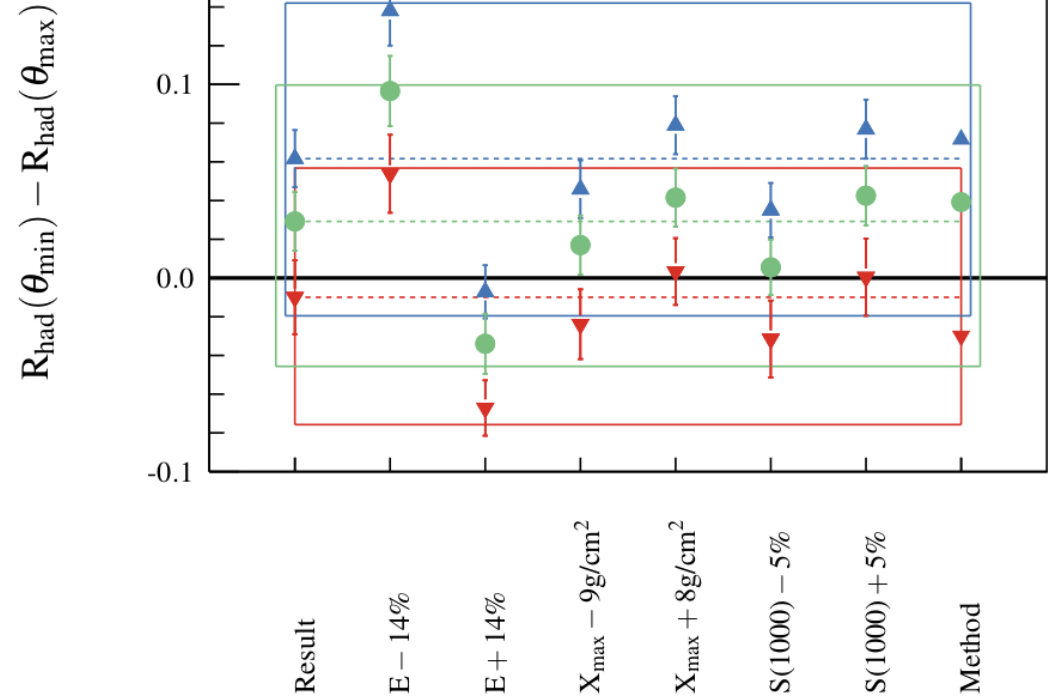
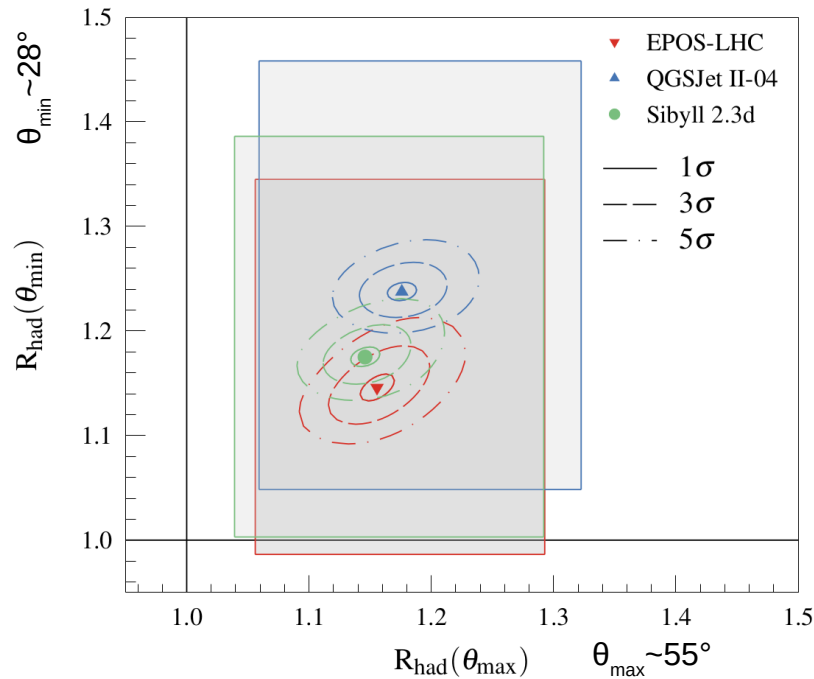


- deeper  $X_{\text{max}}$  predictions for all models !
- alleviated “muon problem“ to ~15-25%
- smaller model differences in mass composition

# Attenuation of hadronic signal with zenith angle

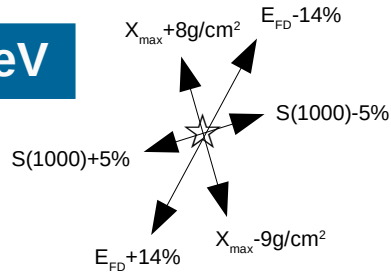
[Phys. Rev. D 109 (2024) 102001]

**10<sup>18.5-19.0</sup> eV**



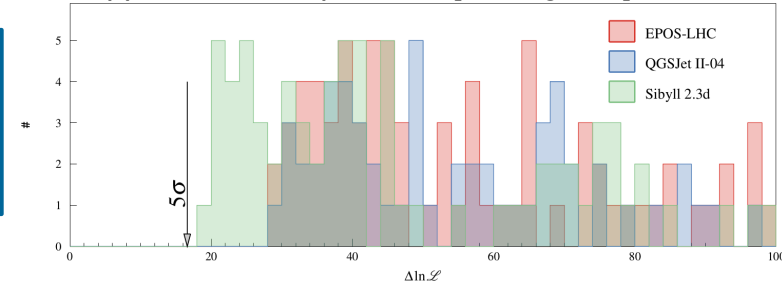
indication of harder muon spectra in QGSJet II-04 than in data

$10^{18.5-19.0}$  eV

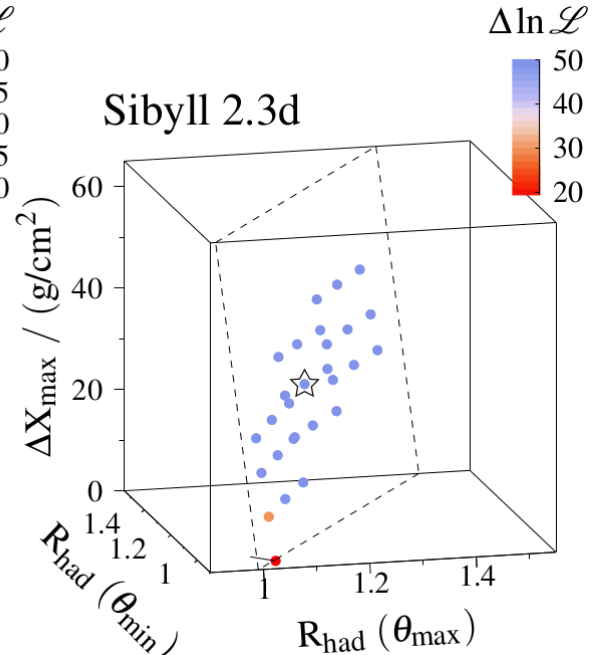
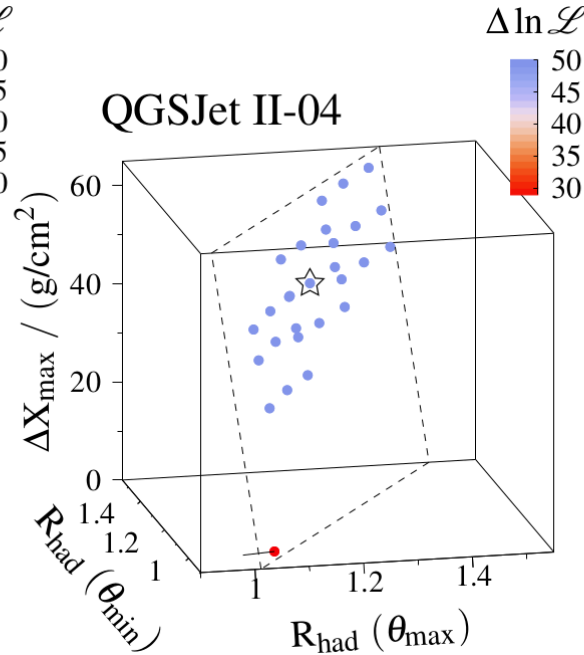
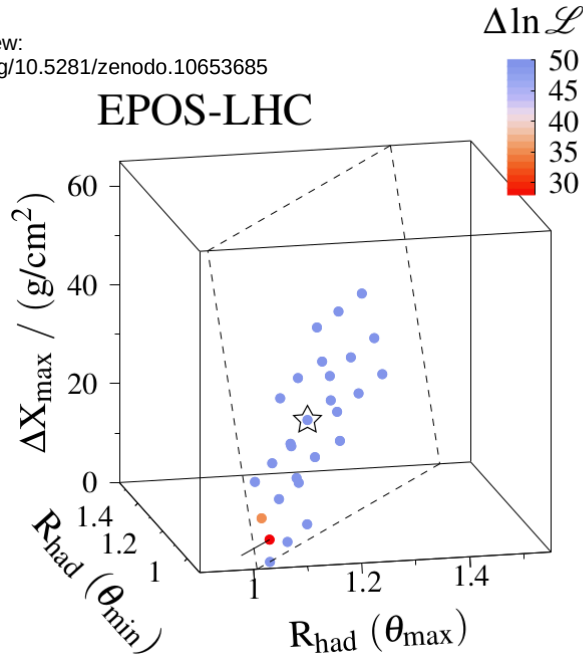


Significance of improvement  
of data description always  
above  $5\sigma$

Denser scan in the region of the closest  
approach of the plane to  $[1,1,0 \text{ g/cm}^2]$



Animated view:  
<https://doi.org/10.5281/zenodo.10653685>



# Summary of tests of models using Auger data

test	energy / EeV	$\theta / ^\circ$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
$X_{\max}$ moments	$\sim 3$ to 50	0 to 80	no tension <span style="color: green;">■</span>	tension <span style="color: red;">■</span>	no tension (2.3c) <span style="color: green;">■</span>
$X_{\max}:S(1000)$ correlation	3 to 10	0 to 60	no tension <span style="color: green;">■</span>	tension <span style="color: red;">■</span>	no tension (2.3c) <span style="color: green;">■</span>
mean muon number	$\sim 10$	$\sim 67$	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>
mean muon number	0.2 to 2	0 to 45	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	—
fluctuation of muon number	4 to 40	$\sim 67$	no tension <span style="color: green;">■</span>	no tension <span style="color: green;">■</span>	no tension <span style="color: green;">■</span>
muon production depth	20 to 70	$\sim 60$	tension <span style="color: red;">■</span>	no tension <span style="color: green;">■</span>	—
$S(1000)$	$\sim 10$	0 to 60	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	—
$[X_{\max}, S(1000)]$ fits	3 to 10	0 to 60	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>

- all models have problems ...
- a need to describe consistently both  $X_{\max}$  and ground signal  
- issue in both observables !



# Summary on tests of models of hadronic interactions

- Indications of a problem to describe Auger data by models in many analyses
  - combinations of measurements of different shower components are powerful tests of models
- Current models of hadronic interactions are proven to fail to describe combined FD+SD data **at 3-10 EeV** with **more than  $5\sigma$**  !
  - possible underestimation of experimental systematics ruled out
  - possibility of a heavier mass composition should be considered
    - alleviation of the “muon problem“ but **start of the “ $X_{\max}$  problem“**
- **New models** of hadronic interactions (EPOS 4(LHCR), QGSJet III, Sibyll\*, Pythia 8, ...) and **new air-shower generator** (CORSIKA 8) are approaching
- **AugerPrime** (2024-2035) will be the best cosmic-ray testing facility for hadronic interactions at  $\sqrt{s} \sim 10\text{-}200$  TeV
- And new methods (Machine Learning) and more data ... Stay tuned !

# Backup slides

# Observables relevant to hadronic interaction models

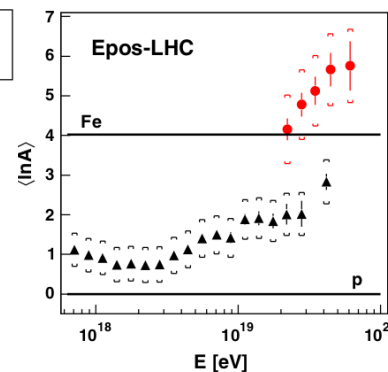
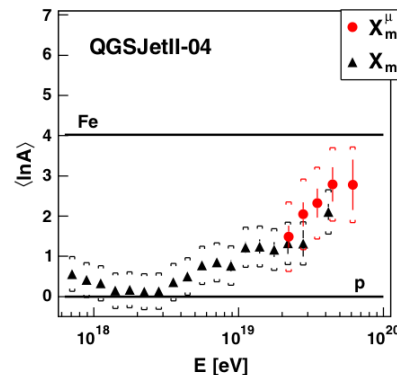
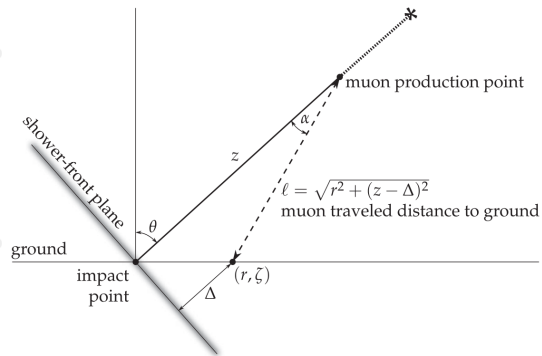
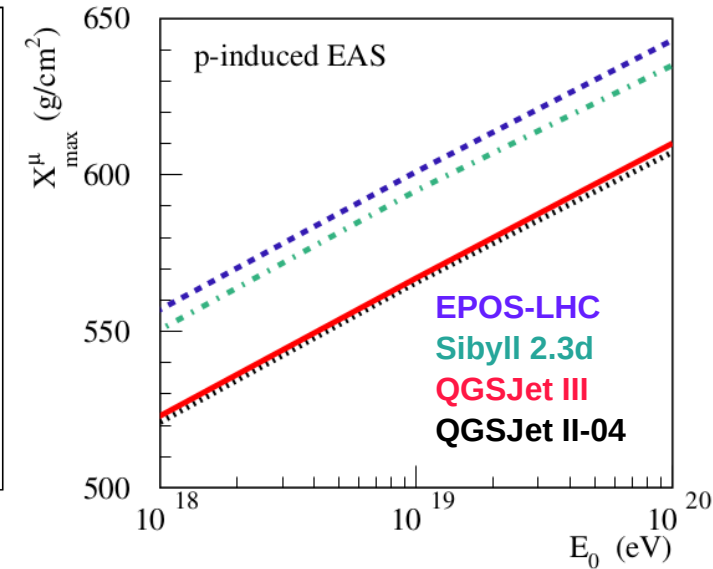
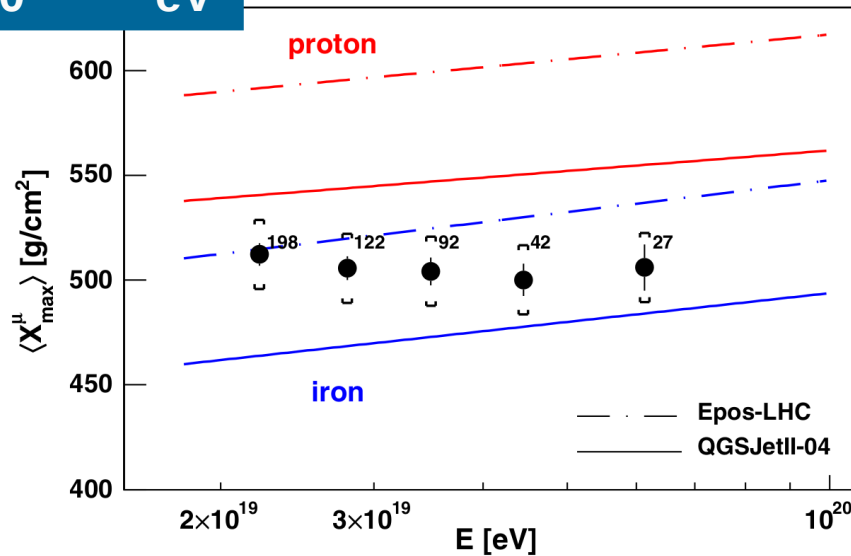
**10<sup>19.3-19.8</sup> eV**

[Phys. Rev. D 90 (2014) 012012]

[Phys. Rev. D 109 (2024) 094019]

## SD signal

- muon content
  - from buried scintillators,  $\theta < 60^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$
- muon production depth
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$



- EPOS-LHC and (likely also) Sibyll 2.3d too deep  $\sim 2\sigma$
- MPD tunable by pion diffraction (loosely constrained by current accelerators data)

# Observables relevant to hadronic interaction models

## SD signal

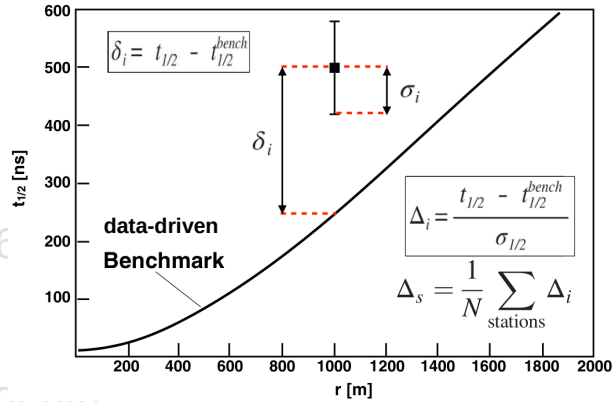
- muon content
- from buried scintillators,  $\theta < 65^\circ$
- from  $N_{19}$ ,  $\theta > 65^\circ$

- muon production  $\Delta_s$
- for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$

- muon energy spectrum
- from attenuation with  $\theta$  and  $r$

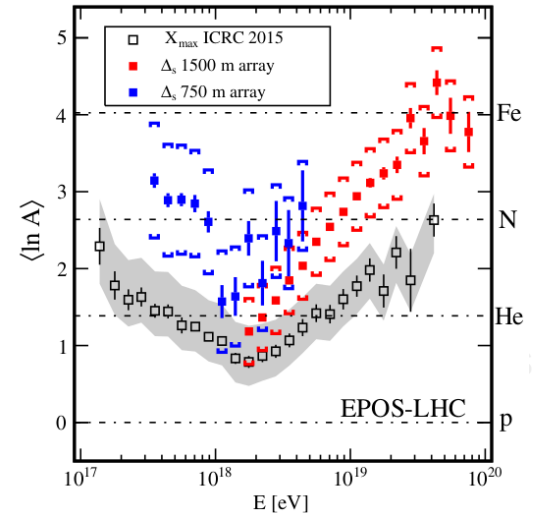
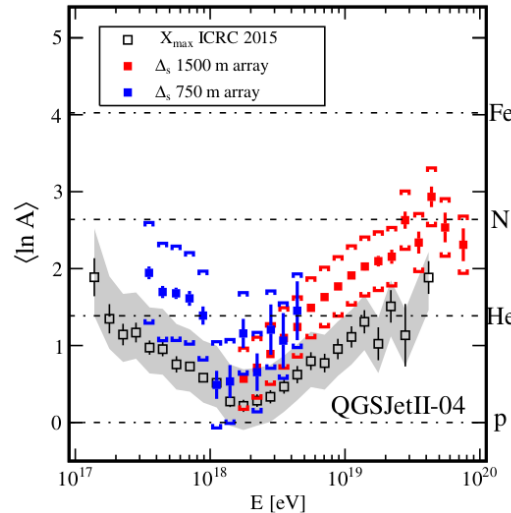
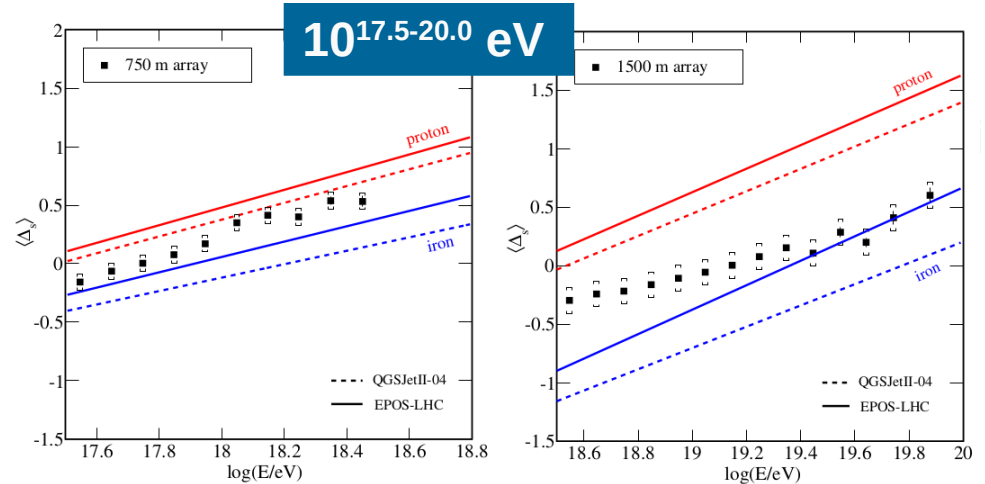
- rise time of signal vs.  $r$

[Phys. Rev. D 96 (2017) 122003]



$$\langle \ln A \rangle = \ln 56 \frac{\langle \Delta_s \rangle_p - \langle \Delta_s \rangle_{\text{data}}}{\langle \Delta_s \rangle_p - \langle \Delta_s \rangle_{\text{Fe}}}$$

**~1-2 $\sigma$  inconsistent interpretation of  $\langle \ln A \rangle$  between  $\Delta_s$  and  $X_{\text{max}}$**



# Observables relevant to hadronic interaction models

[JCAP 03 (2019) 018]

**10<sup>17.8-19.5</sup> eV**

## SD signal

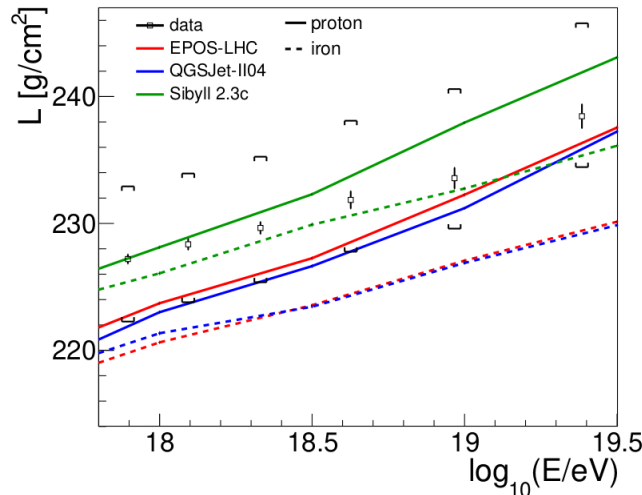
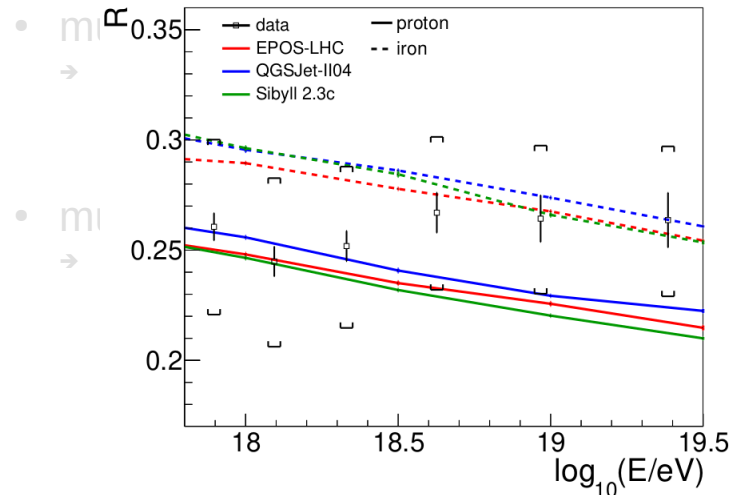
$$f_{GH}(X) = (dE/dX)_{\max} \left( \frac{X - X_0}{X_{\max} - X_0} \right)^{\frac{X_{\max} - X_0}{\lambda}} \exp \left( -\frac{X_{\max} - X}{\lambda} \right)$$

$$(dE/dX)' = \left( 1 + R \frac{X'}{L} \right)^{R-2} \exp \left( -\frac{X'}{RL} \right)$$

## FD longitudinal profile

- muon content
- from buried scintillators,  $\theta < 60^\circ$
- from  $N_{19}$ ,  $\theta > 65^\circ$

- so far consistent within  $\sim 2\sigma$  with models
- smaller systematics on aerosol measurement could improve constraints



- average shape of longitudinal profiles

# Observables relevant to hadronic interaction models

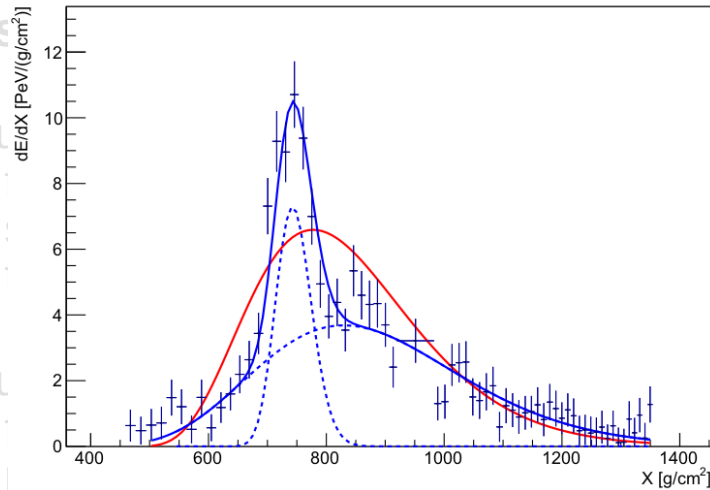
[EPJ Web Conf. 144 (2017) 01009]

FD profile

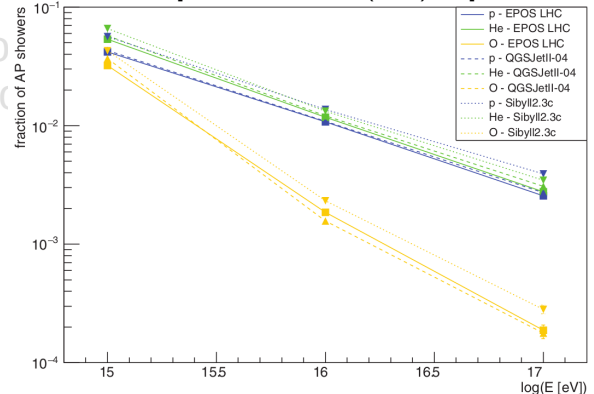
**$10^{17.2-18.5}$  eV ?**

**FD longitudinal profile**

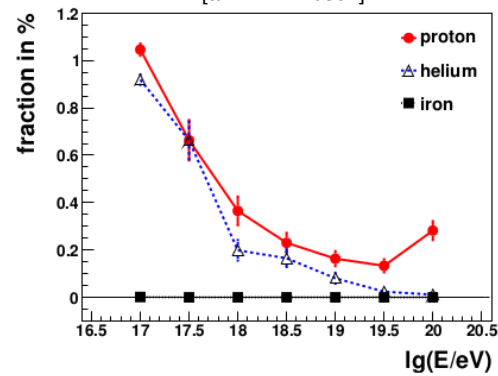
- % effect at  $10^{18}$  eV, % effect at  $10^{16}$  eV
- hard to reject presence of clouds
  - ➔ additional cloud measurement is needed
- possible constraints on presence of lightest primaries (and cross-section/elasticity)
- no application to the data yet



[Astron. Nachr. 340 (2019) 234]



[arXiv:1111.0504]

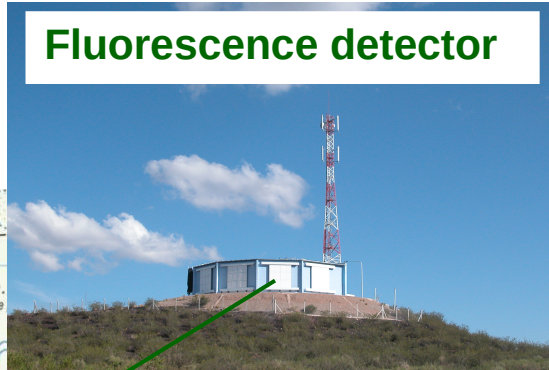


- average shape of longitudinal profiles
- frequency of **anomalous showers**

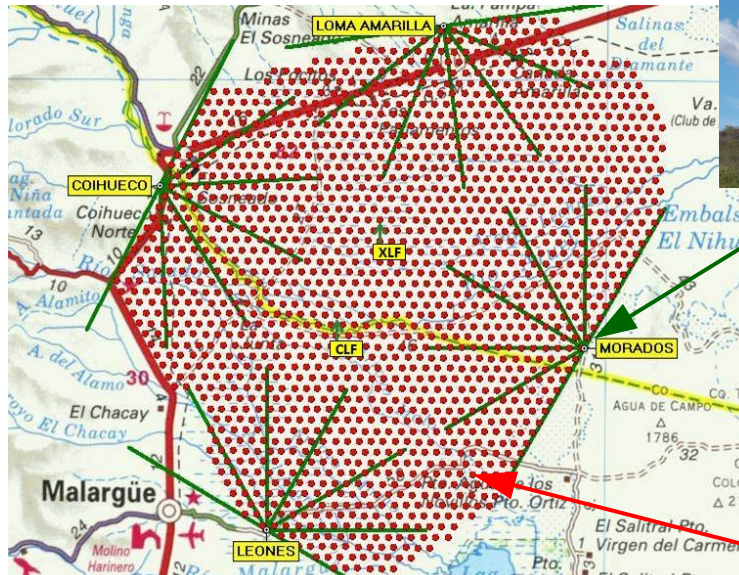
[EPJ Web of Conferences 144 (2017) 01009]

# Hybrid detection at the Pierre Auger Observatory

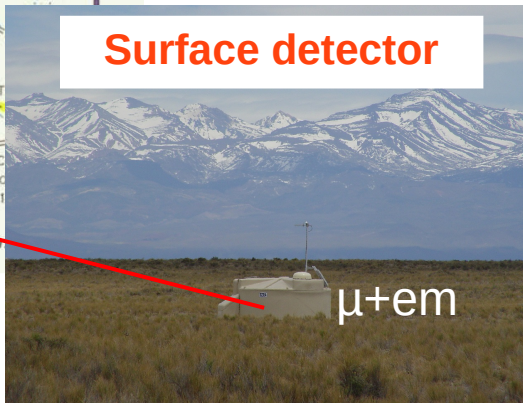
Fluorescence detector



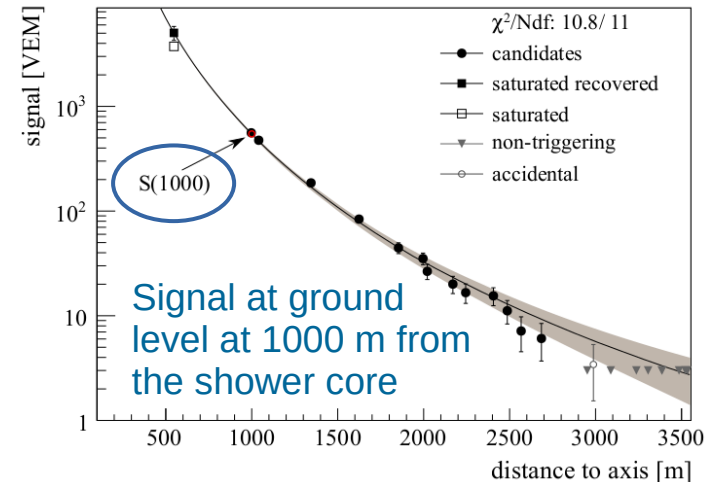
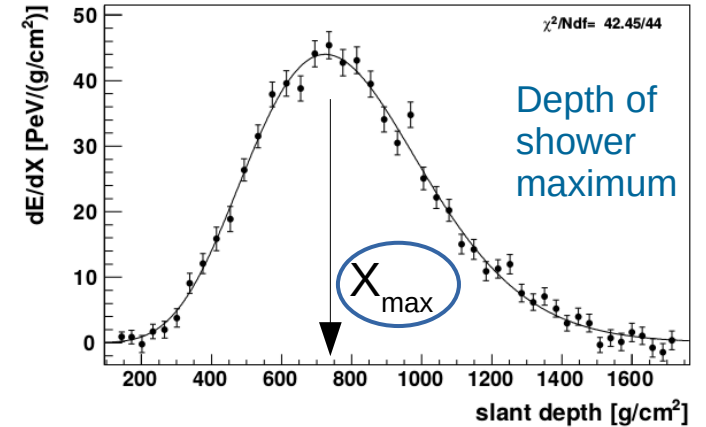
[Nucl. Instrum. Meth. A 798 (2015) 172]



Surface detector



$\mu+em$



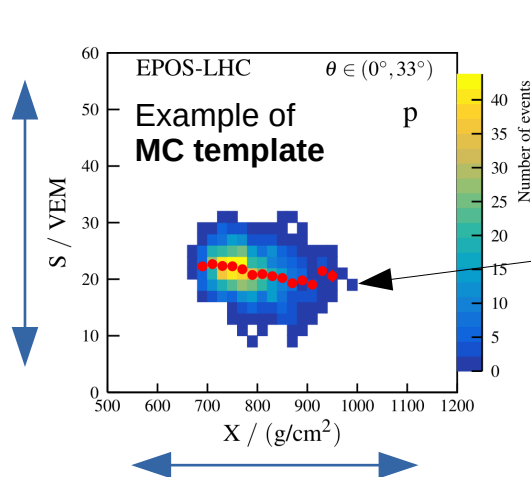
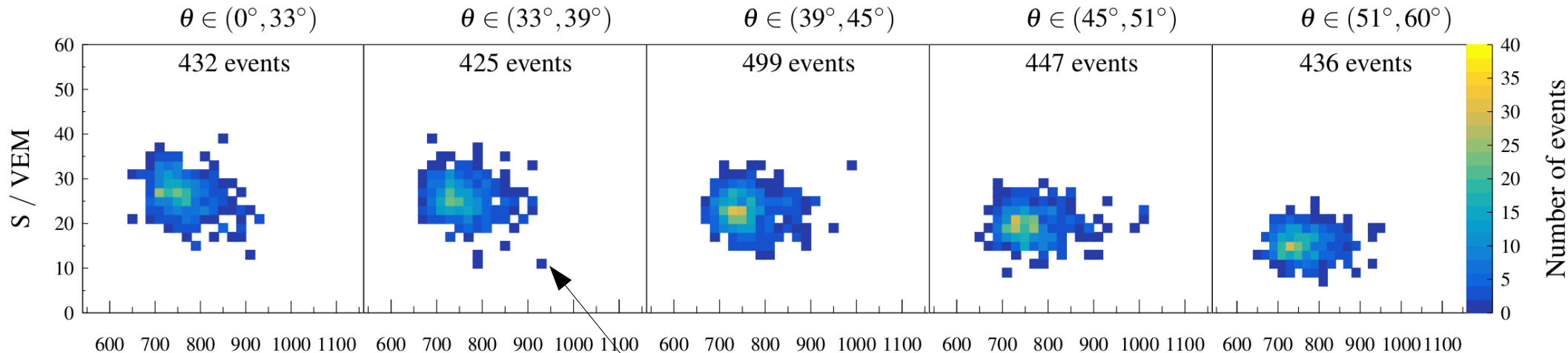
**Auger data:**  
2239 HQ events for  $10^{18.5-19.0}$  eV

# Method

$$S = S(1000) \left( \frac{E^{\text{ref}}}{E_{\text{FD}}} \right)^{1/B}$$

$$X = X_{\text{max}} + D \lg \left( \frac{E^{\text{ref}}}{E_{\text{FD}}} \right)$$

$E^{\text{ref}} = 10^{18.7}$  eV



$$\ln \mathcal{L} = \begin{cases} \sum_k \sum_j (C_{jk} - n_{jk} + n_{jk} \ln \frac{n_{jk}}{C_{jk}}), & n_{jk} > 0 \\ \sum_k \sum_j C_{jk}, & n_{jk} = 0 \end{cases}$$

$\theta$  bins  
2D bins

- Freedom in  $X_{\text{max}}$  ( $\Delta X_{\text{max}}$ ) and  $S(1000)$  ( $R_{\text{had}}(\theta)$ ) and primary fractions
- Change of  $S_{\text{had}}$  and  $S_{\text{em}}$  due to  $\Delta X_{\text{max}}$  incorporated

Simultaneous log-likelihood ratio fit of **two-dimensional distributions** of  $X_{\text{max}}$  and  $S(1000)$  in 5 zenith-angle bins with **MC templates** for combinations of four primary nuclei (p, He, O, Fe)



# Motivations for modifications of MC predictions

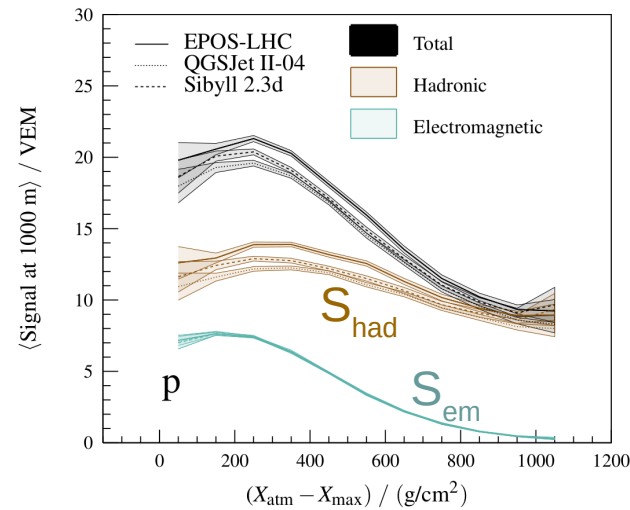
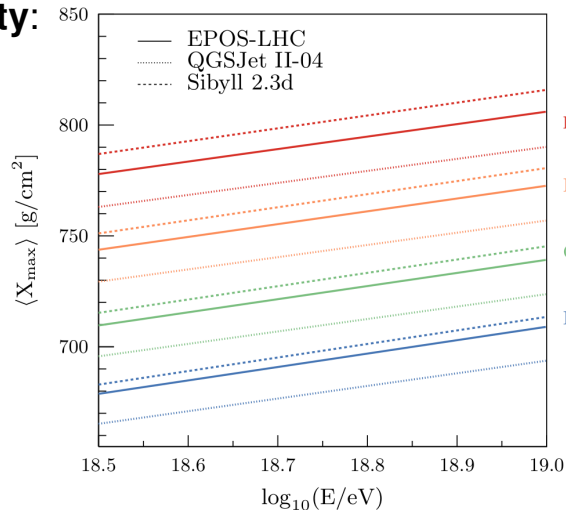
- Properties of **4-component shower universality**:

[Astropart. Phys. 87 (2017) 23, Astropart. Phys. 88 (2017) 46]

- $S(1000) = S_{had} + S_{em}$
- $S_{em}$  very universal

- **Main differences** between model predictions:

- Scale of  $\langle X_{max} \rangle$  and  $\langle S_{had} \rangle(\theta)$  are **approx. primary and energy independent**



$$X_{atm} = 880 / \cos \theta \text{ g/cm}^2$$

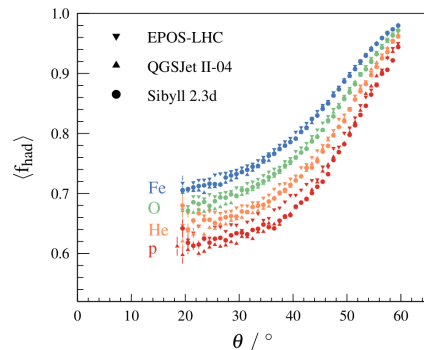
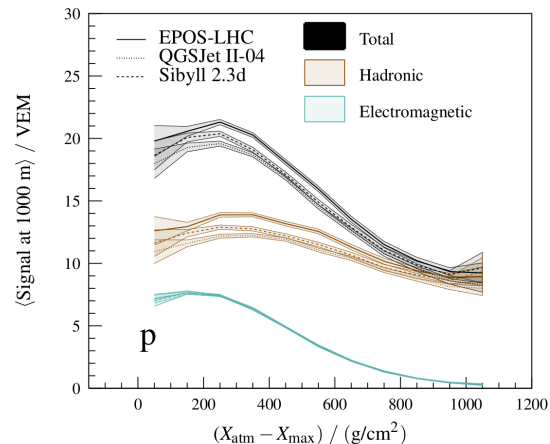
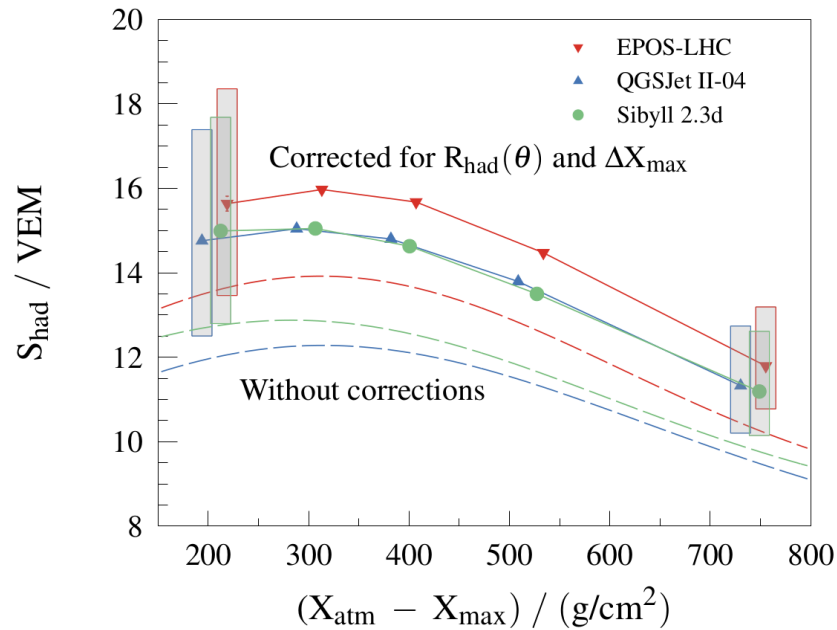
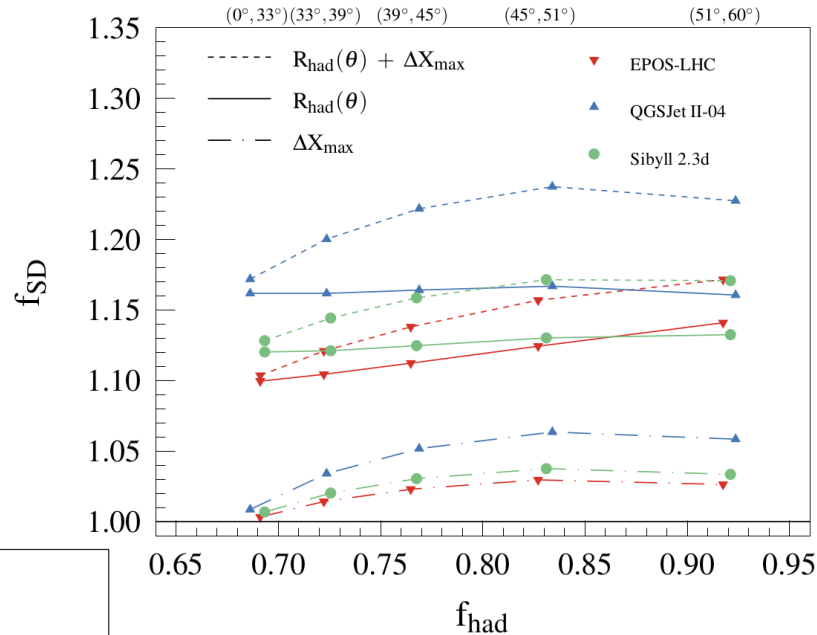
**Caveat:** no modifications in fluctuations or mass-dependencies etc. considered

## ad-hoc modifications

$$X_{max} \rightarrow X_{max} + \Delta X_{max}$$

$$S_{had}(\theta) \rightarrow S_{had}(\theta) \cdot R_{had}(\theta)$$

# Effect of modified $X_{\max}$ on the ground signal



# Assumption on primary species

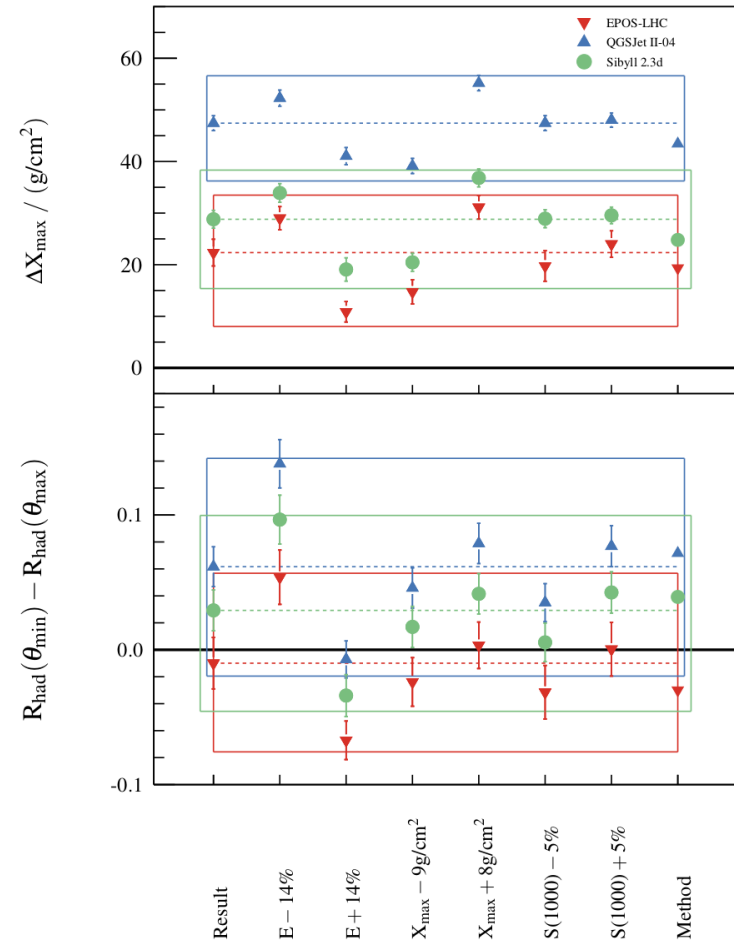
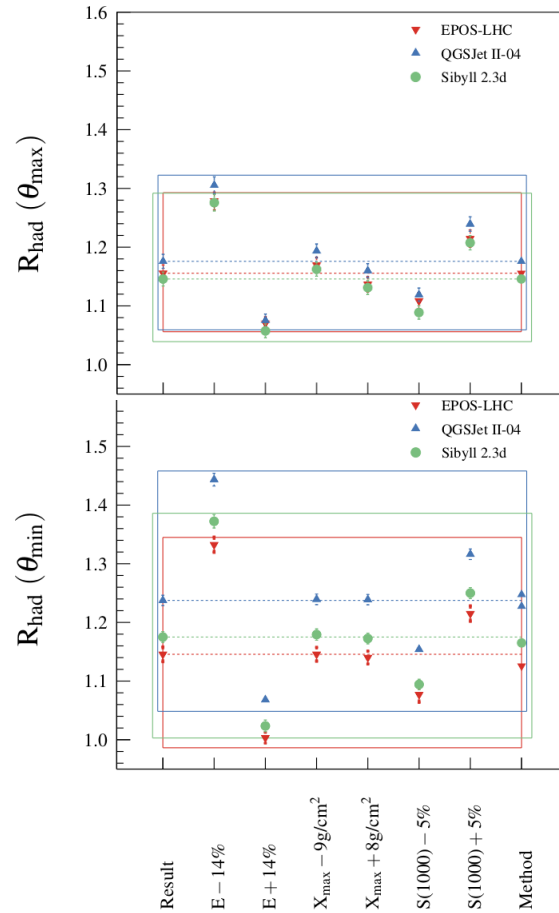
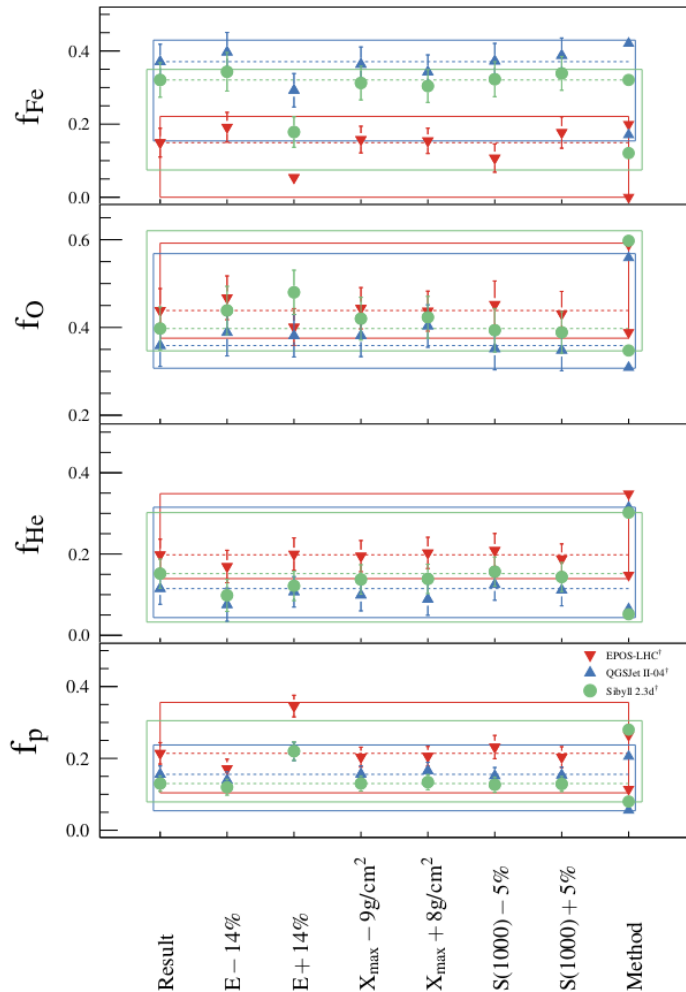
- $\Delta X_{\max}$  decreases by about 5-7, 10-17 and 30-40 g/cm<sup>2</sup> and  $R_{\text{had}}(\theta)$  increases by about 2-5%, 4-9% and 15-20% when the heaviest primary Fe is replaced by Si, O and He, respectively

$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
p He	518.3	633.5	563.5
p He O	467.5	523.3	486.6
p He O Fe	451.9	476.3	451.6

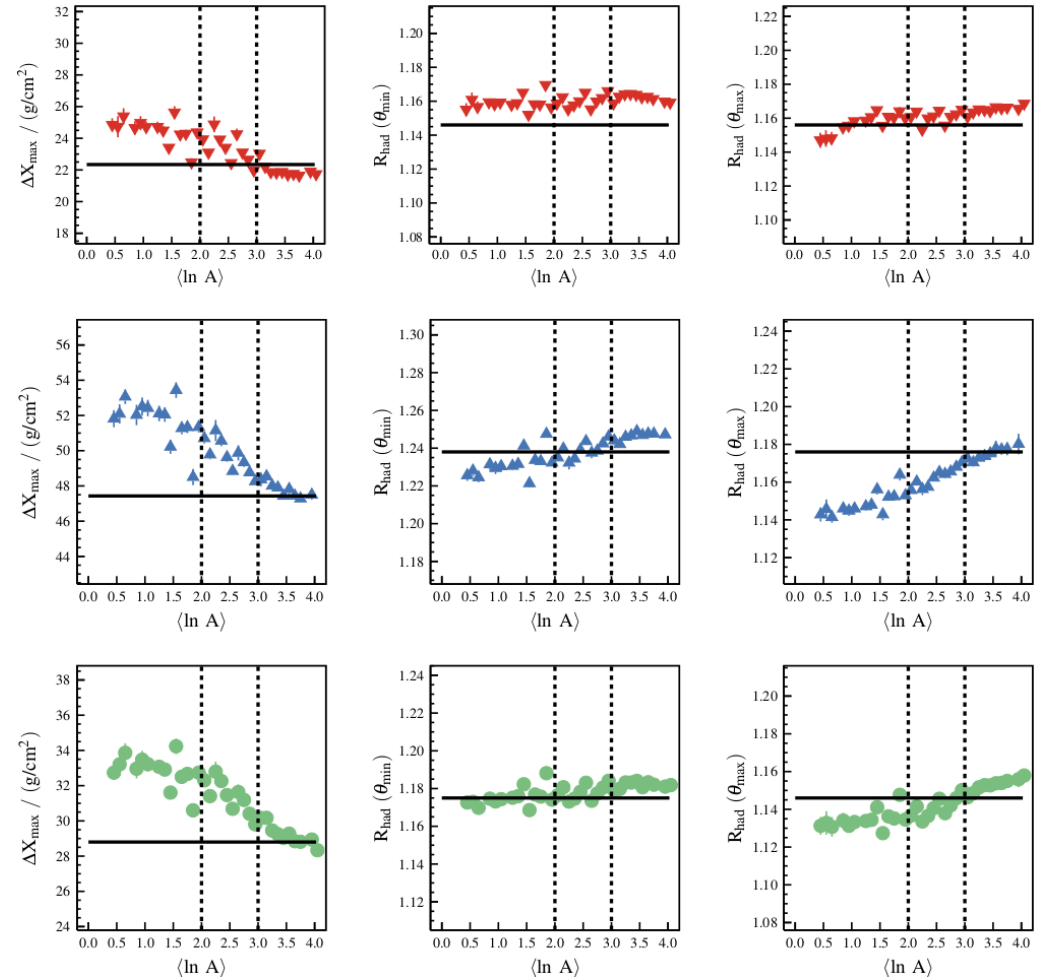
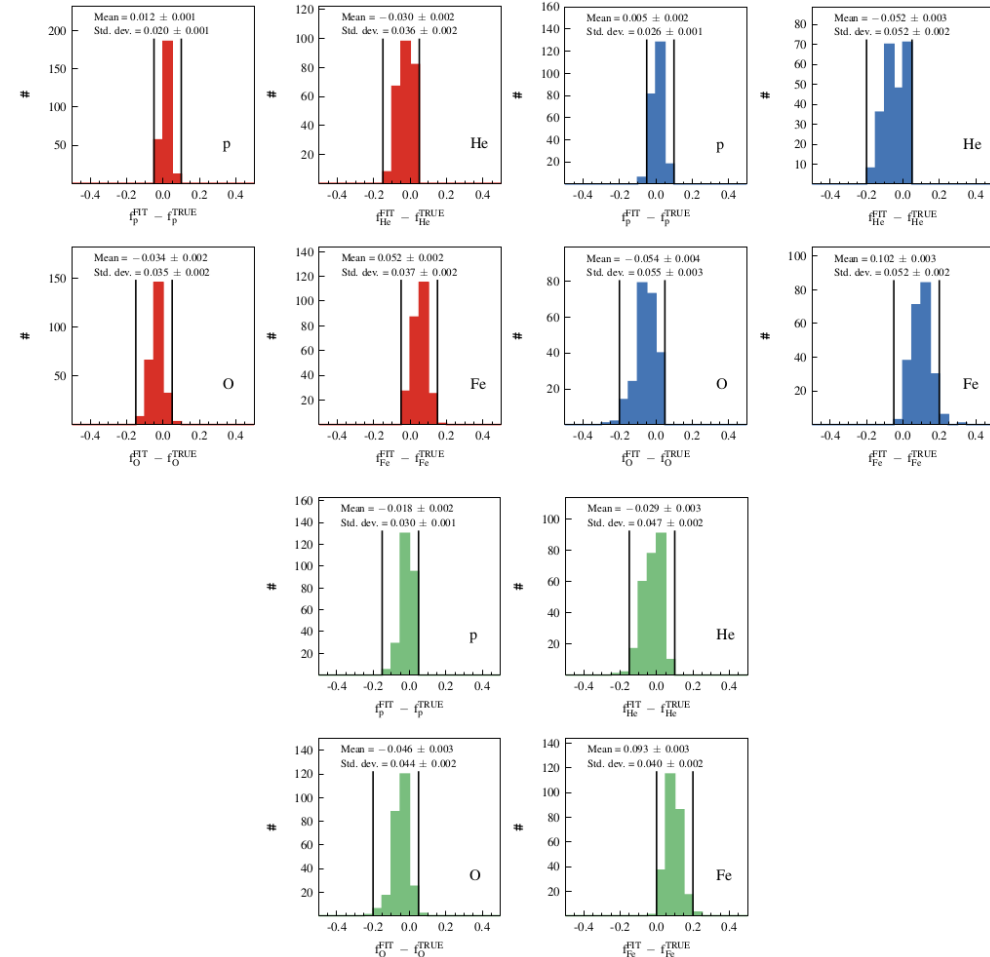


Significance of improvement of data description above  $5\sigma$

# Systematic uncertainties

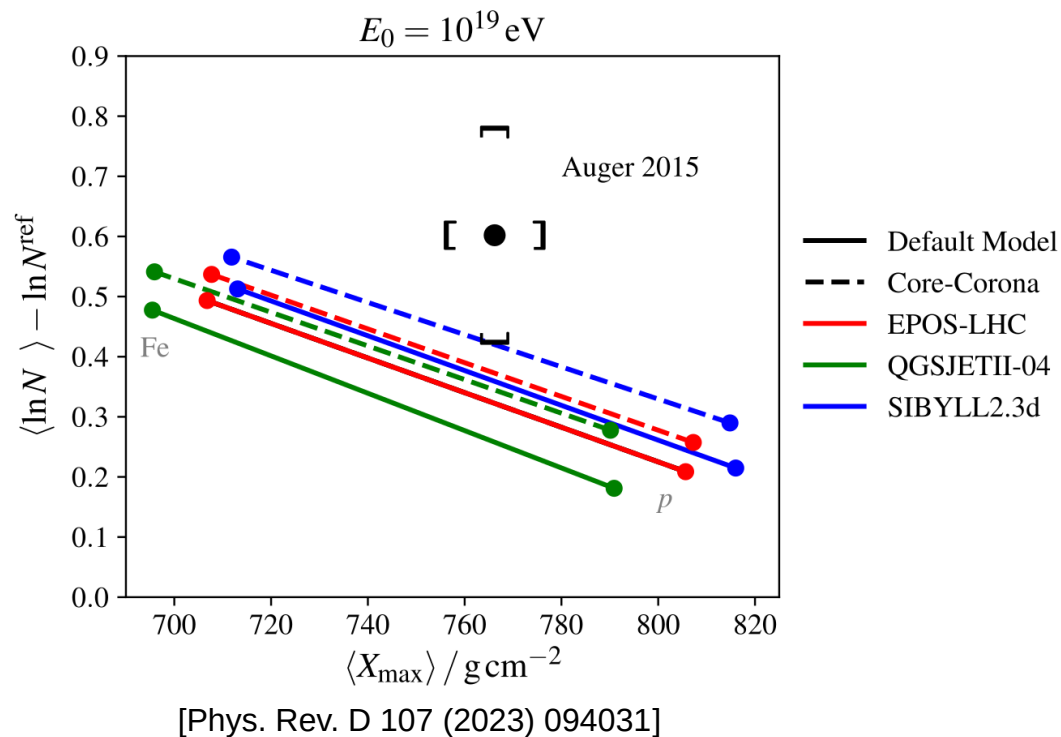


# MC-MC tests

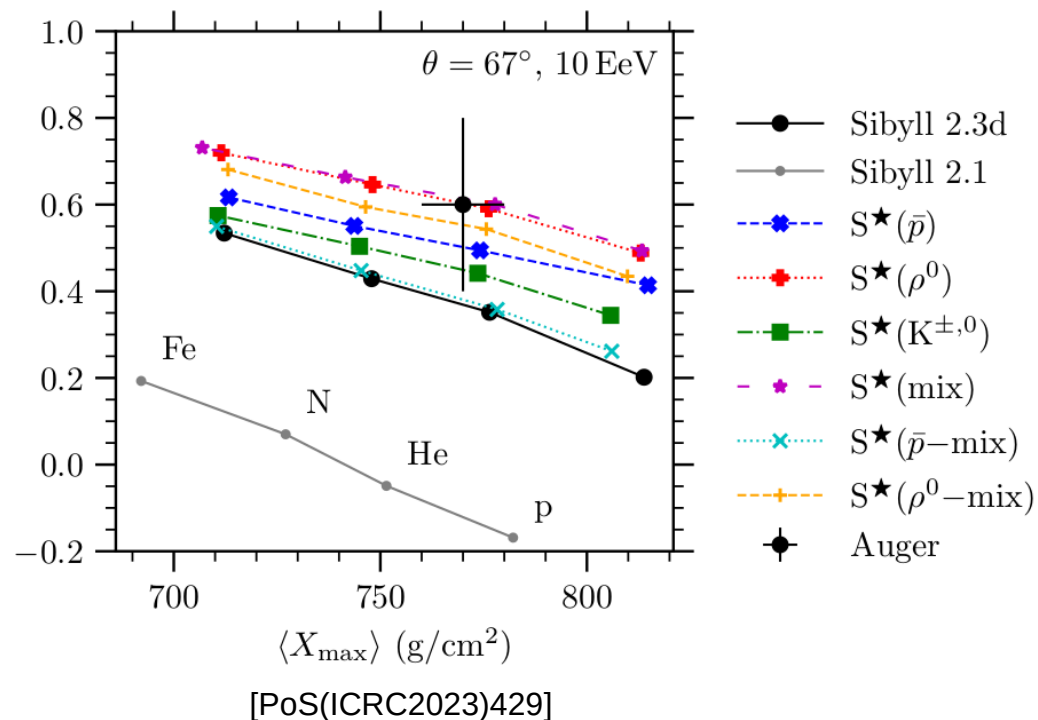


# Adding muons ~ without changing $X_{\max}$

Core-corona model - collective statistical hadronization → EPOS 4

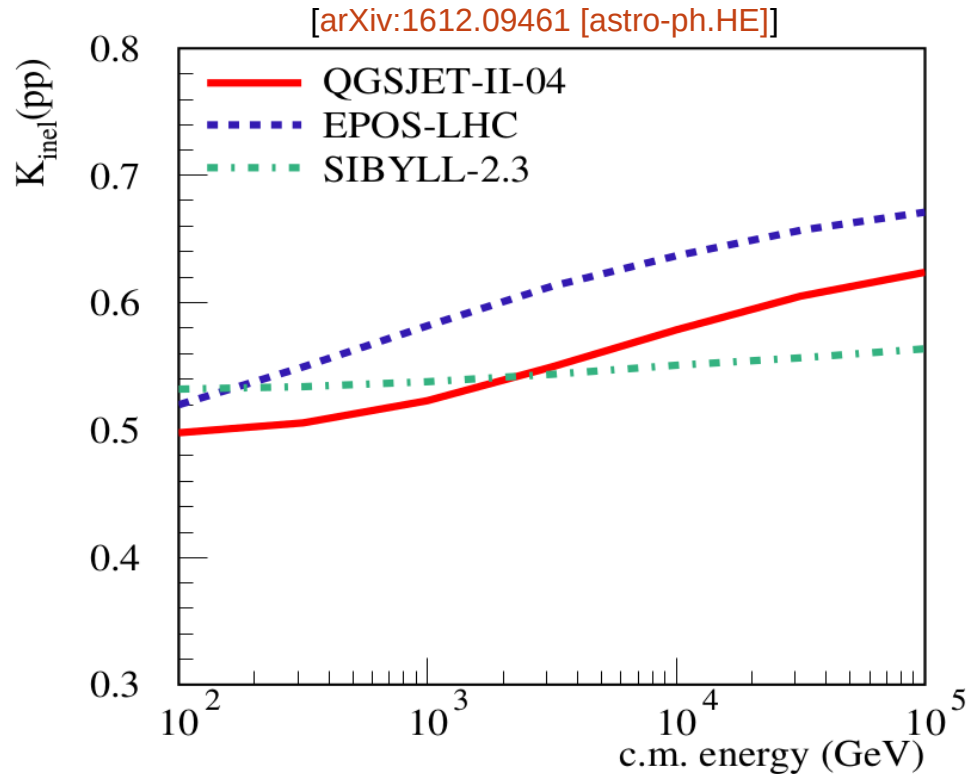


Sibyll \* - artificial enhancement of muons



# Possible mass-(in)dependence of $X_{\max}$ shift

“changing the normalization of energy dependence”  $\rightarrow$  mass independent modifications



multiplicity:  $N \propto N_0 \cdot E^\alpha$   
 inelasticity:  $\kappa \propto \kappa_0 \cdot E^{-\omega}$

$$X_{\max}^A = X_1^A + X_0 \ln \frac{\kappa E}{A \cdot 2N \xi_C^\pi} =$$

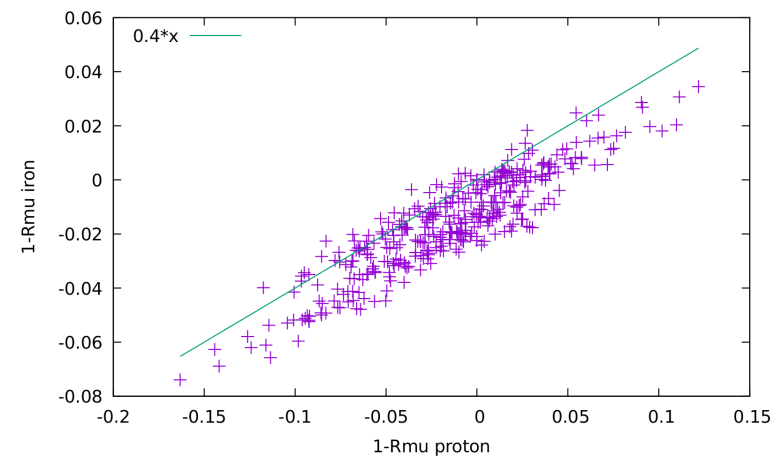
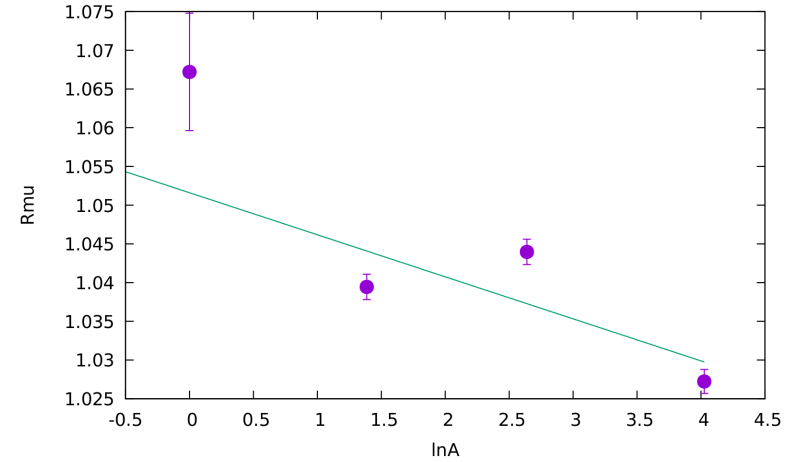
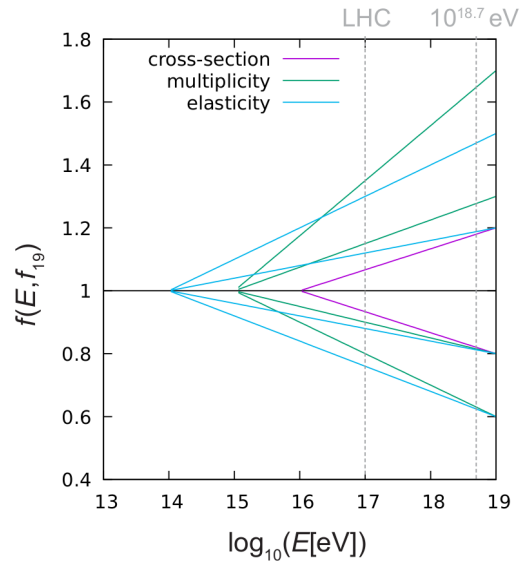
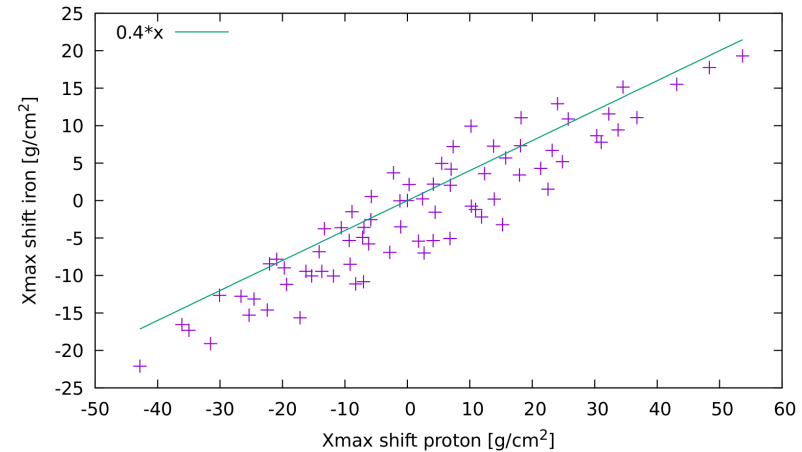
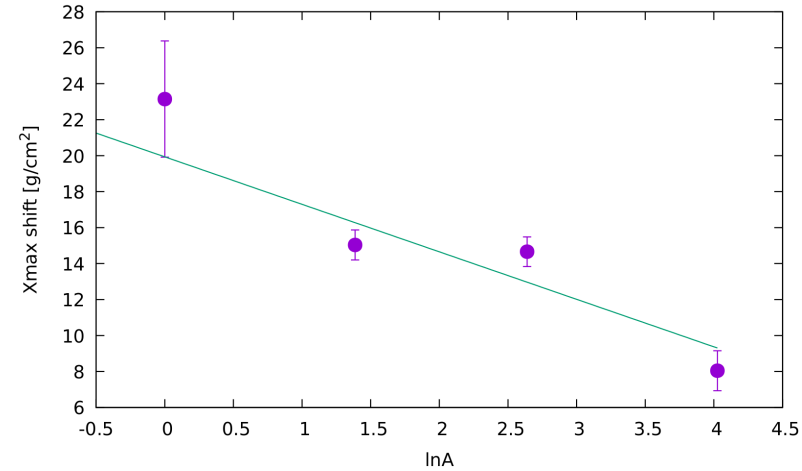
$$X_1^A + (1 - \alpha - \omega) \cdot \left( X_0 \ln \frac{E}{A \cdot \xi_C^\pi} \right) + X_0 \cdot (\ln \kappa_0 - \ln N_0)$$

$$\begin{matrix} \kappa_0 \rightarrow f_\kappa \kappa_0 \\ N_0 \rightarrow f_N N_0 \end{matrix} \Rightarrow X_{\max}^A{}' = X_{\max}^A + X_0 (\ln(f_\kappa) - \ln(f_N))$$

# MOCHI (preliminary)

[PoS(ICRC2023)245]

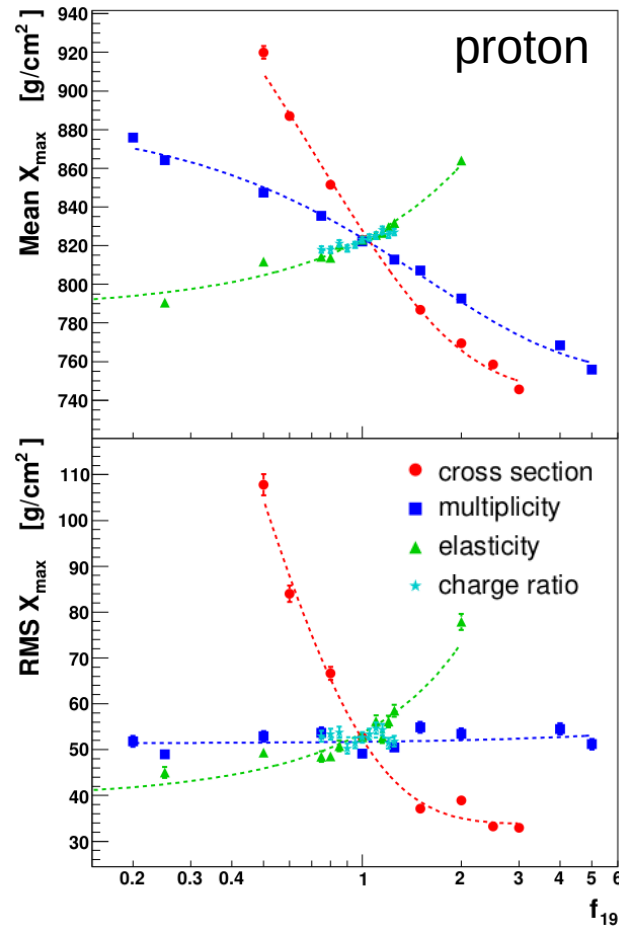
“changing the shape of energy dependence” → mass-dependent modifications



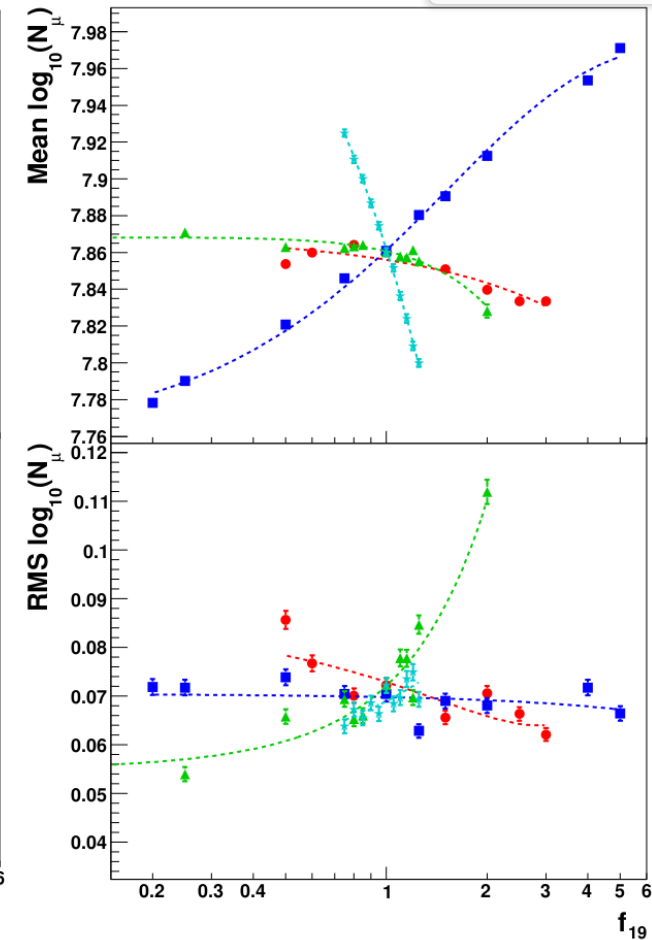


# Modifications of hadronic interactions

- 1D CONEX simulations
- Sibyll 2.1 @  $10^{19.5}$  eV
- Cross-section modification, or resampling of produced particles
- Energy threshold for modifications  $10^{15}$  eV



[Phys. Rev. D 83 (2011) 054026]



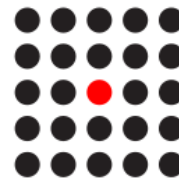
# Towards more complex explanation: MOCHI

## *MO*modified *C*haracteristics of *H*adronic *I*nteractions

- CONEX in CORSIKA: 3D information
- Modification factors in **cross-section**, **multiplicity** and **elasticity**

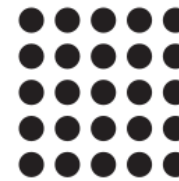


0.8

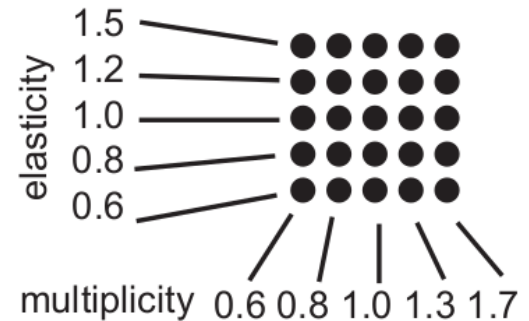


1.0

cross-section



1.2



- **MOCHI library:**

- Sibyll 2.3d
- energy  $10^{18.7}$  eV
- protons and iron nuclei
- 5 zenith angles
- 1000 showers per „bin“
- 750 000 showers (~200 TB, ~250y CPU time)

*See [PoS(ICRC2023)245]  
for more detail*

# Range of modifications and thresholds

## Cross-section ( $E_{\text{thr}} = 10^{16}$ eV)

- well constrained for p-p at LHC to a few %
- unc. in conversion to p-A limited by CMS p-Pb measurement

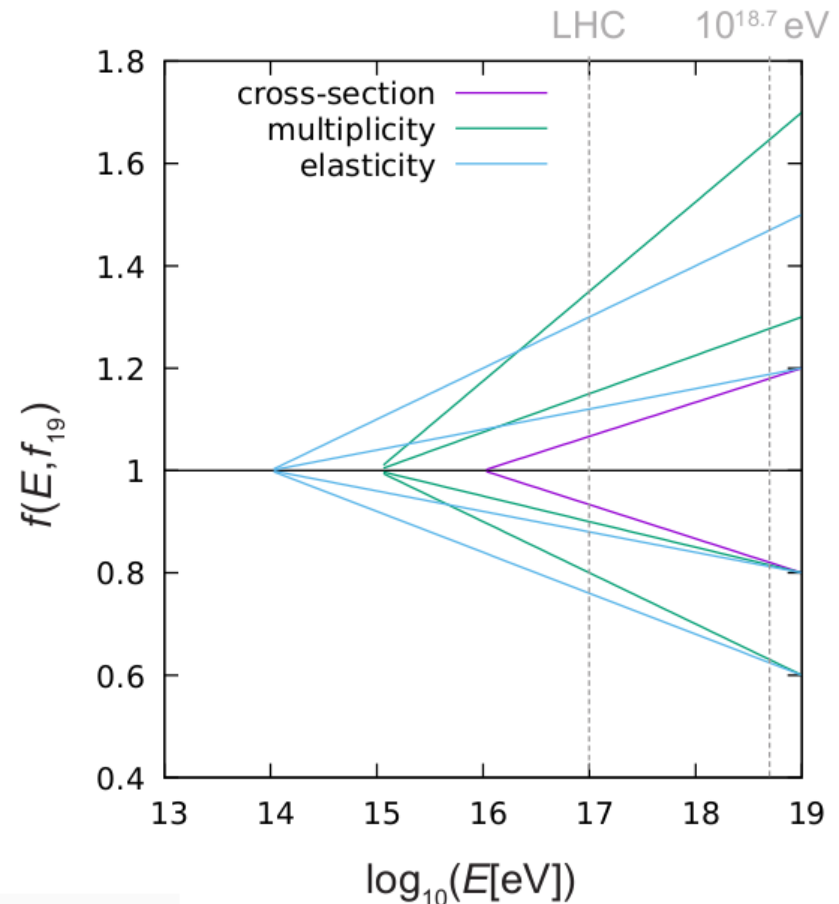
## Multiplicity ( $E_{\text{thr}} = 10^{15}$ eV)

- no p-A data, limited rapidity coverage

## Elasticity ( $E_{\text{thr}} = 10^{14}$ eV)

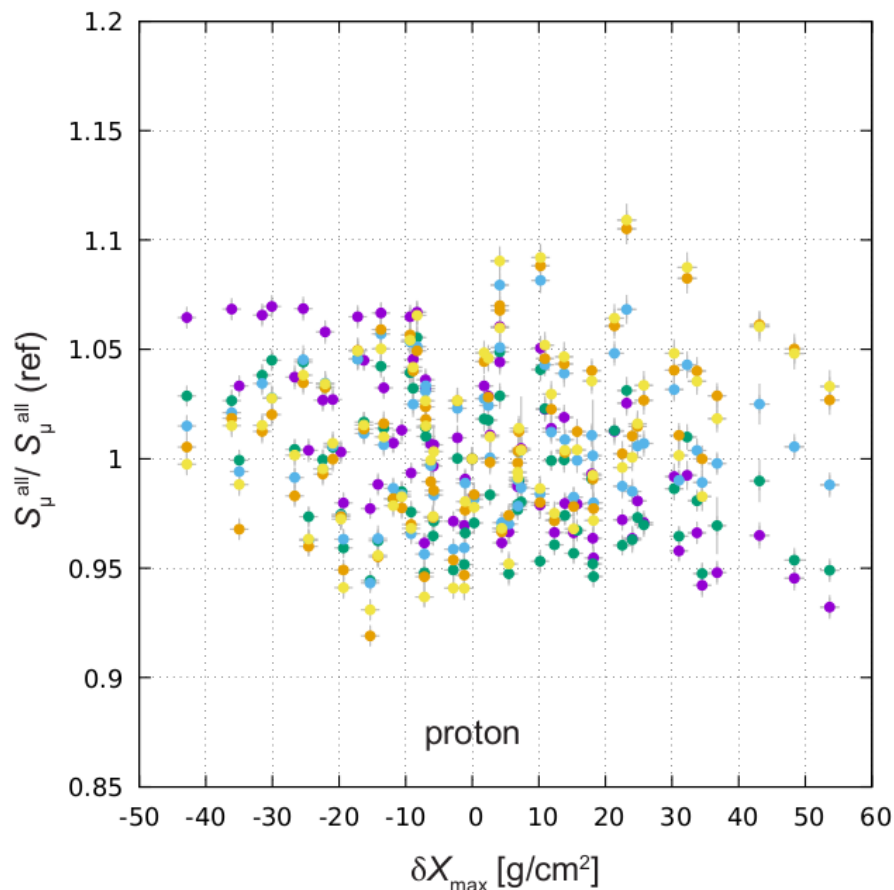
- difficult at accelerators, limits from nuclear emulsion chambers
- recent LHCf neutron elasticity measurement?
- range of modifications limited by internal consistency

$$f(E, f_{19}) = 1 + (f_{19} - 1) \cdot \frac{\log_{10}(E/E_{\text{thr}})}{\log_{10}(10 \text{ EeV}/E_{\text{thr}})}$$

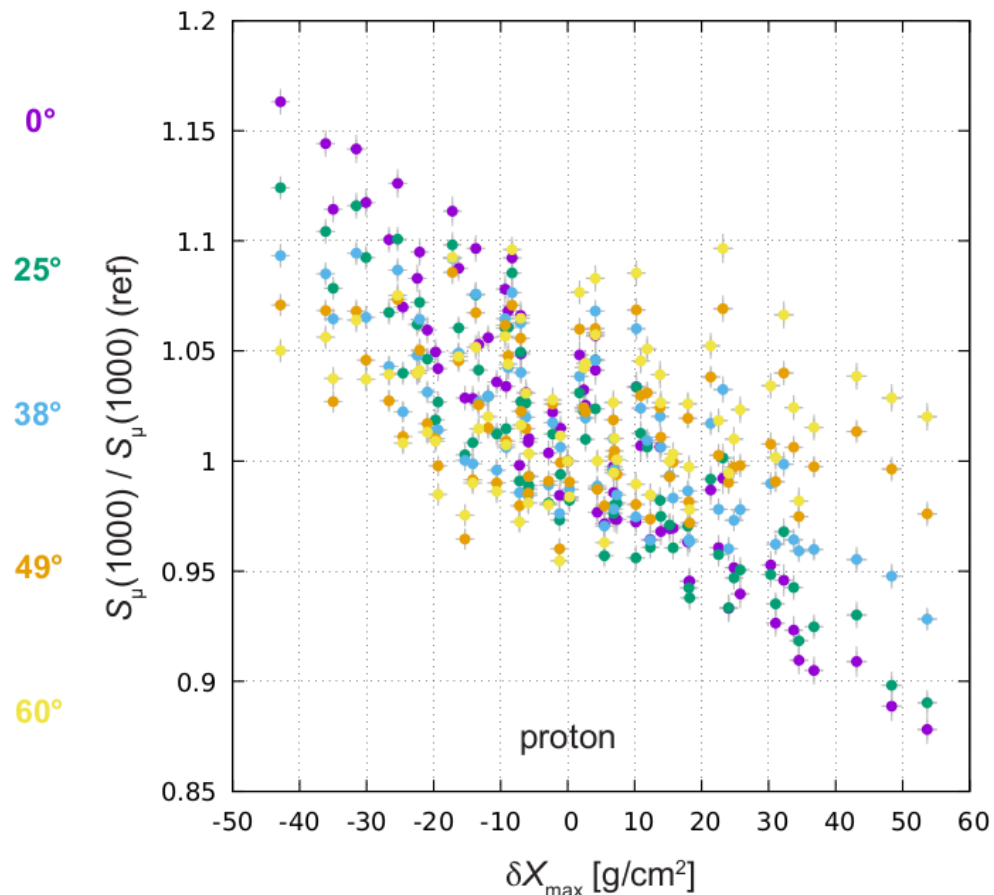


# Importance of 3D simulation

## All muons

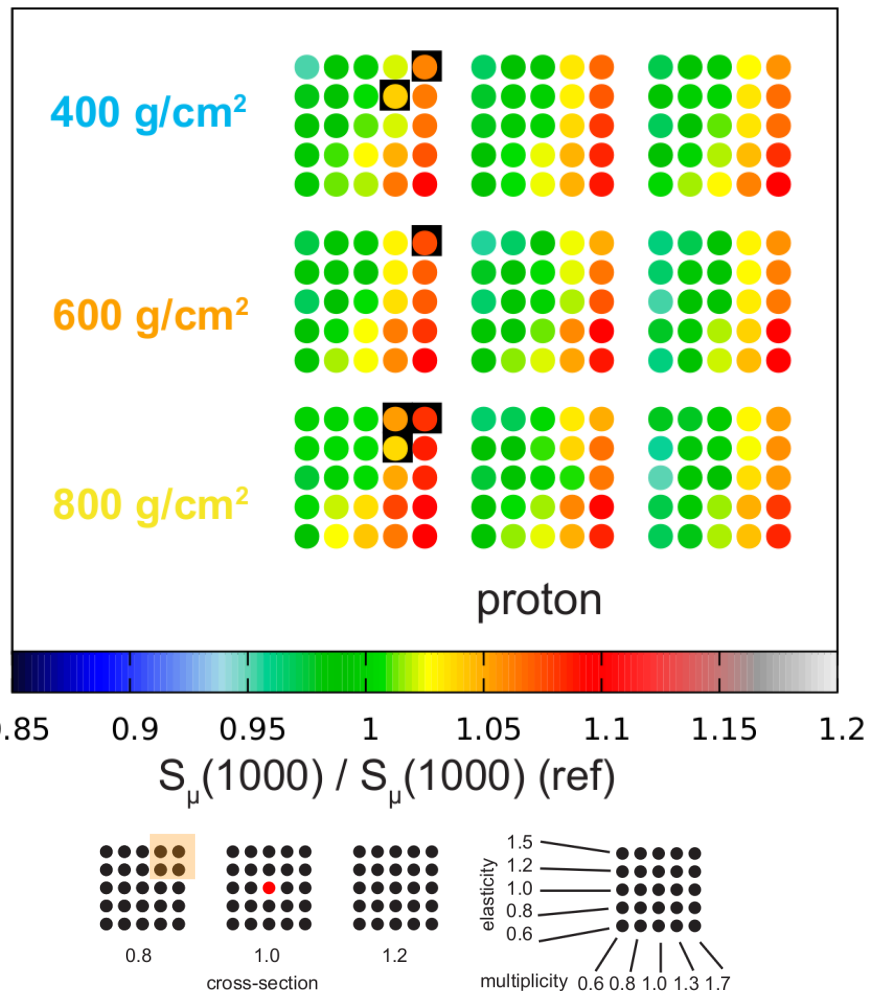
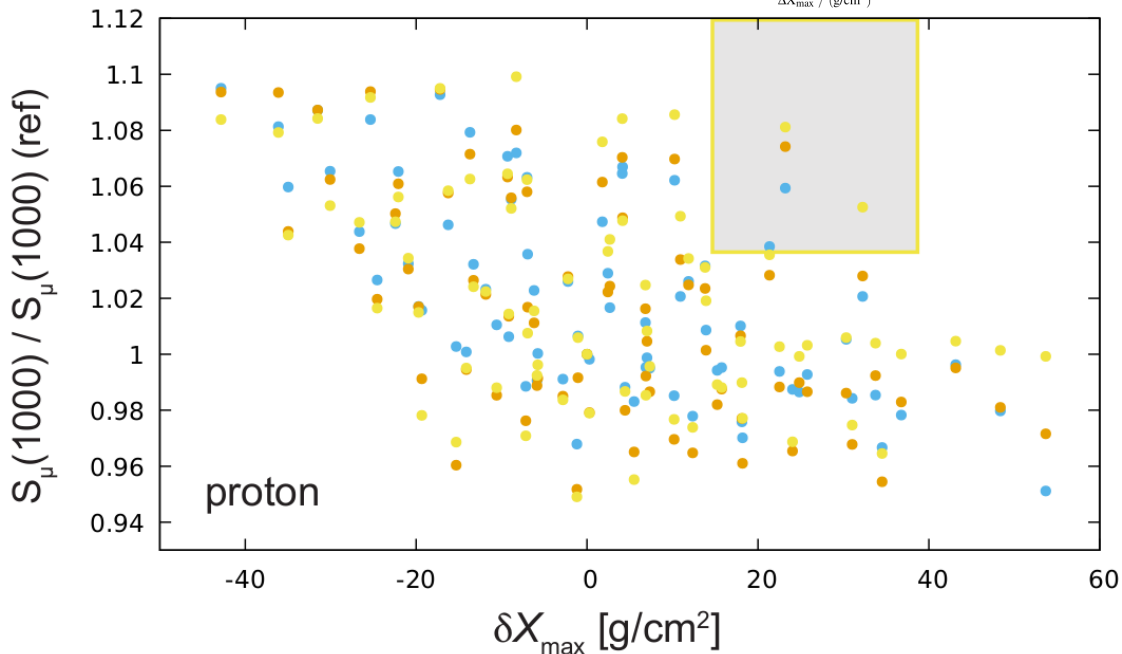
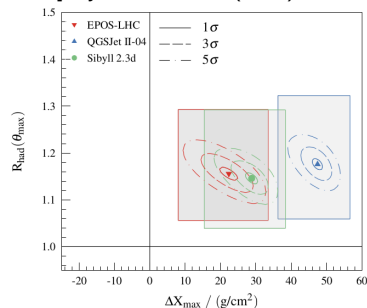


## Muons around 1000m

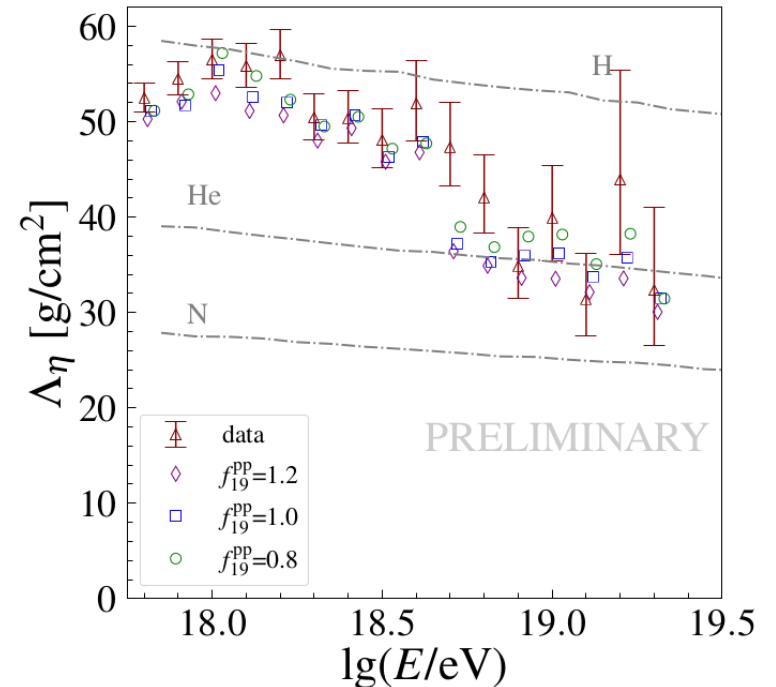
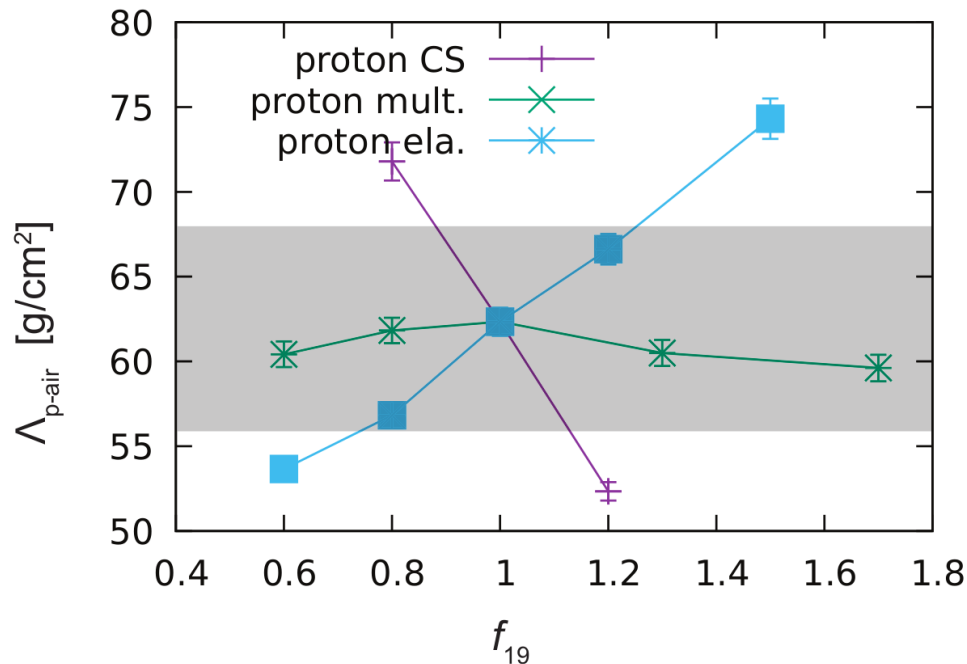


# Comparison with Auger results

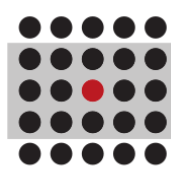
[Phys. Rev. D 109 (2024) 102001]



# Effect on tail of $X_{\max}$ distribution

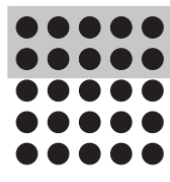


0.8



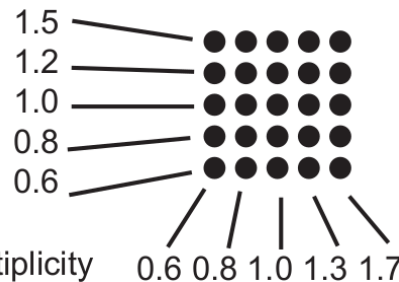
1.0

cross-section



1.2

elasticity

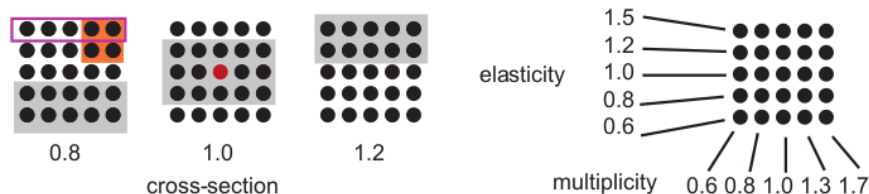
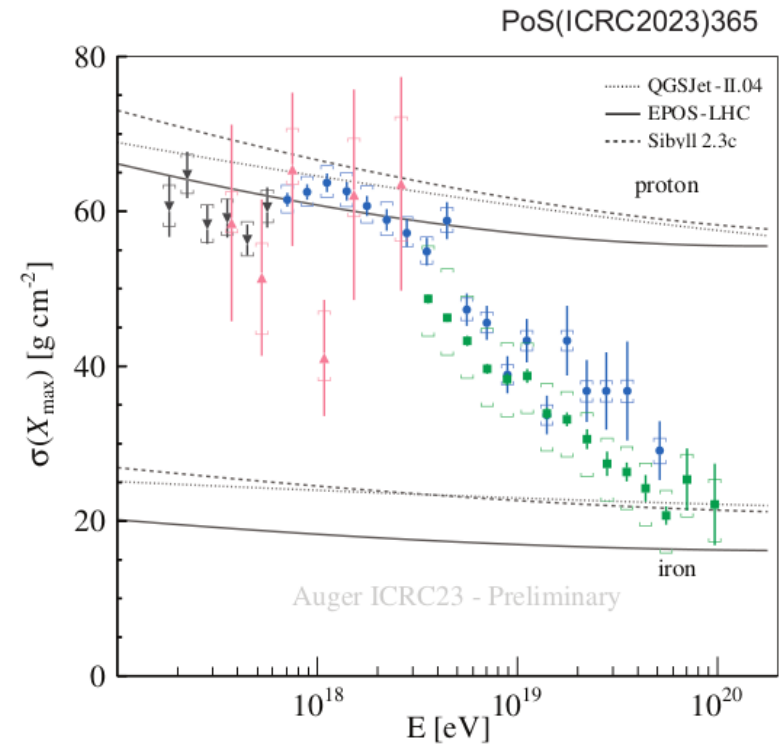
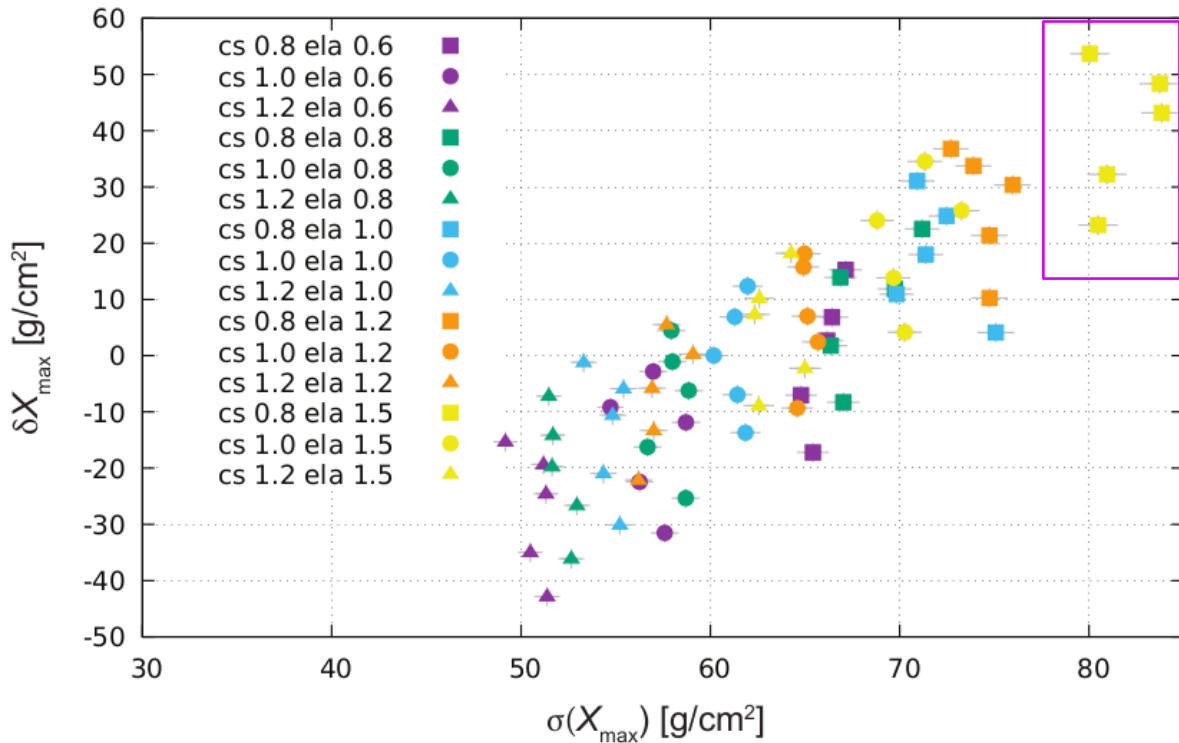


multiplicity

0.6 0.8 1.0 1.3 1.7

Slope of  $X_{\max}$  tail distribution for protons too constrained by Auger data

# Effect on $X_{\max}$ fluctuations



Lower cross-section and high elasticity leads to very high  $X_{\max}$  fluctuations that may be difficult to reconcile with data